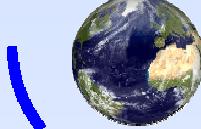
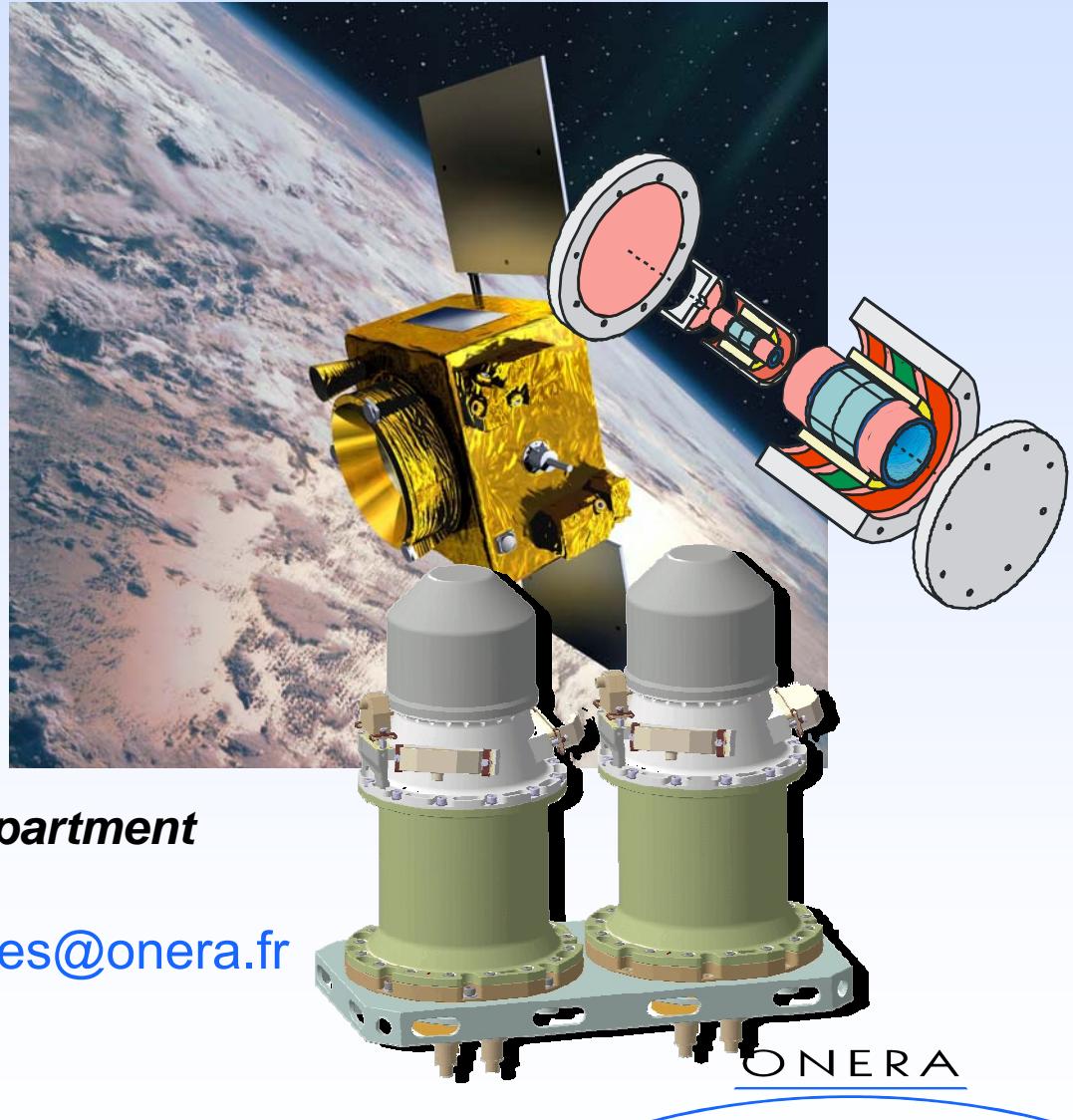


**GREX 2004 : NICE 27 - 29 octobre 2004**



**MICROSCOPE  
MISSION &  
INSTRUMENT**

*Pierre Touboul & Manuel Rodrigues*  
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# MICROSCOPE Team

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## ZARM Bremen

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B. Pouilloux, P. Prieur, P.G. Tizien, O. Vandermarcq, et al.

## ESA

D. Nicolini

# Testing the EP on ground

From Eötvös Experiment To:

- In laboratory:

- Baessler S., Heckel B., Alderberger E., Gundlach J.,...
- Eotwash project : Torsion pendulum
- Washington State University

$$\left\langle \left[ \frac{M_G}{M_I} \right]_E - \left[ \frac{M_G}{M_I} \right]_M \right\rangle_{wep} = (0.1 \pm 4.4) \times 10^{-13}$$

$$[a_{\text{Earth}} + a_{\text{Moon}}]/2 = 5.93 \times 10^{-3} \text{ ms}^{-2} \text{ (toward the Sun)}$$

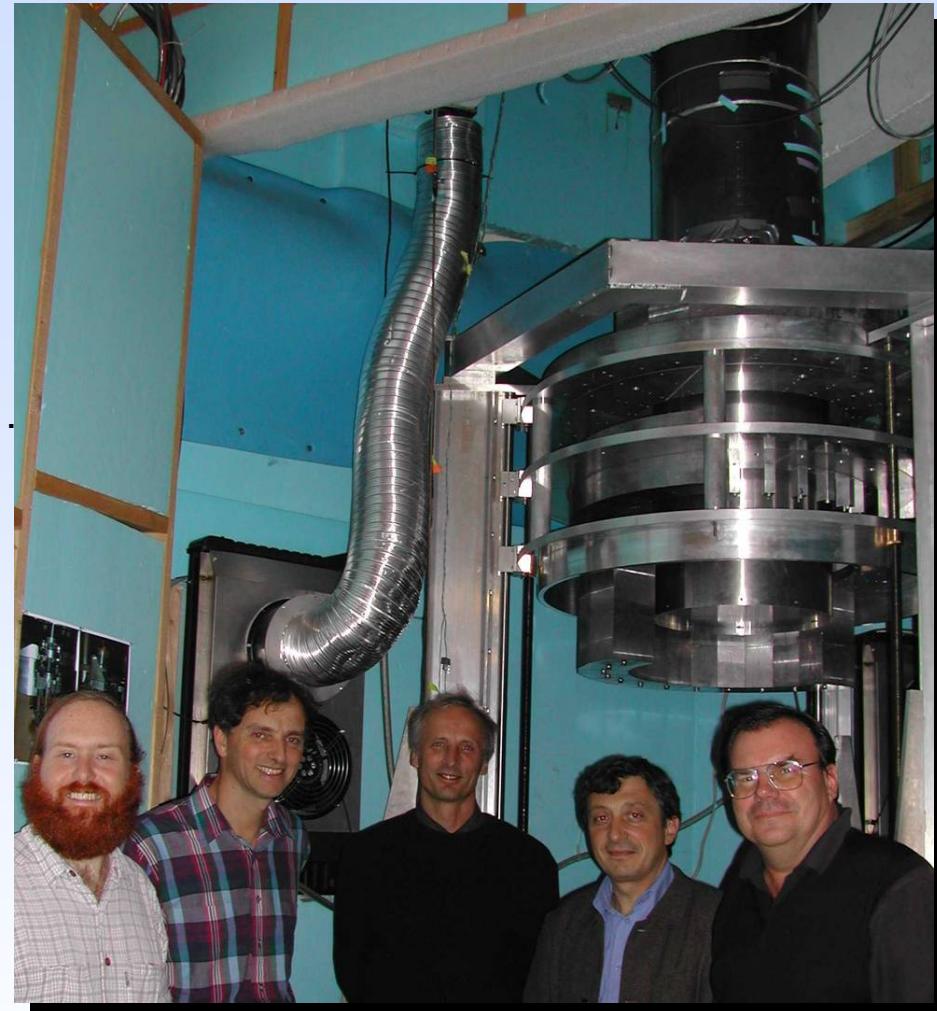
Ref:

Short-range tests of the equivalence principle

G. L. Smith, C. D. Hoyle, J. H. Gundlach, E. G. Adelberger, B. R. Heckel, and H. E. Swanson

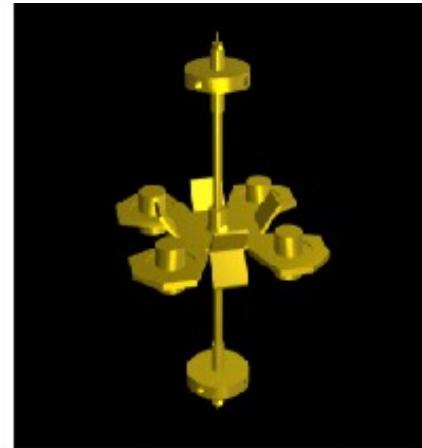
*Department of Physics, University of Washington, Seattle, Washington 98195*

*PHYSICAL REVIEW D, VOLUME 61, 022001*



# Testing the EP on ground

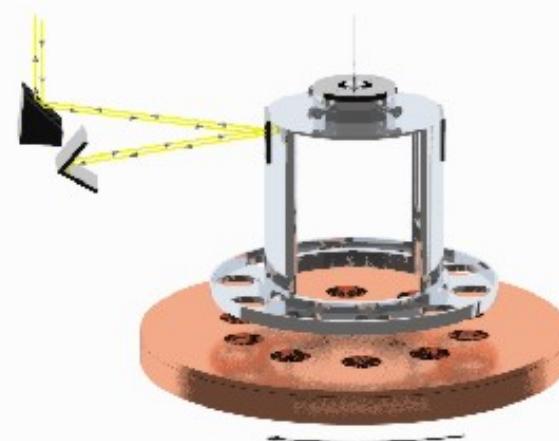
- Eotwash project : Torsion pendulum - *Washington State University*



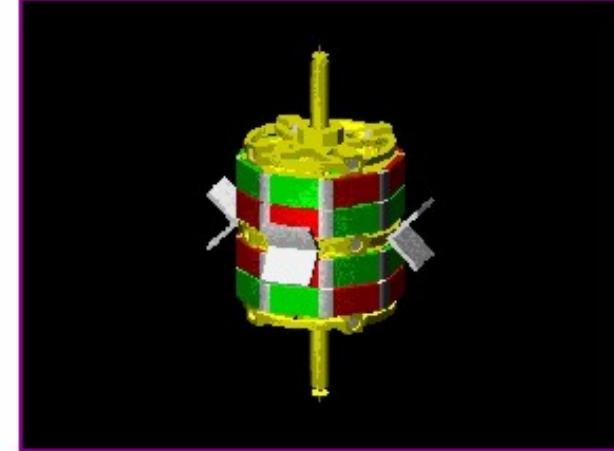
Torsion Pendulum used in the Rot-Wash Instrument



8-Body Torsion Pendulum used in the Eöt-Wash III Instrument



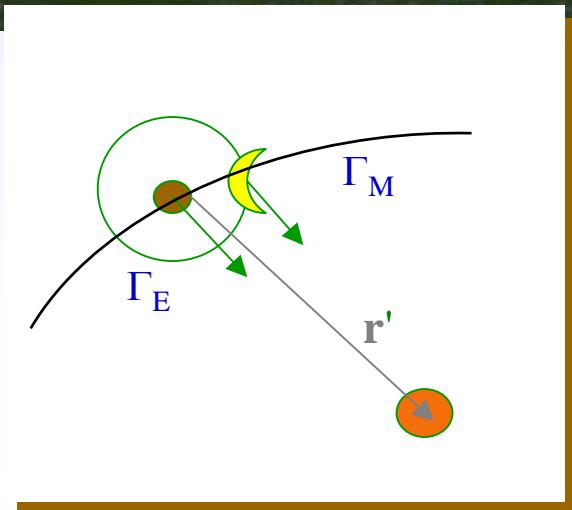
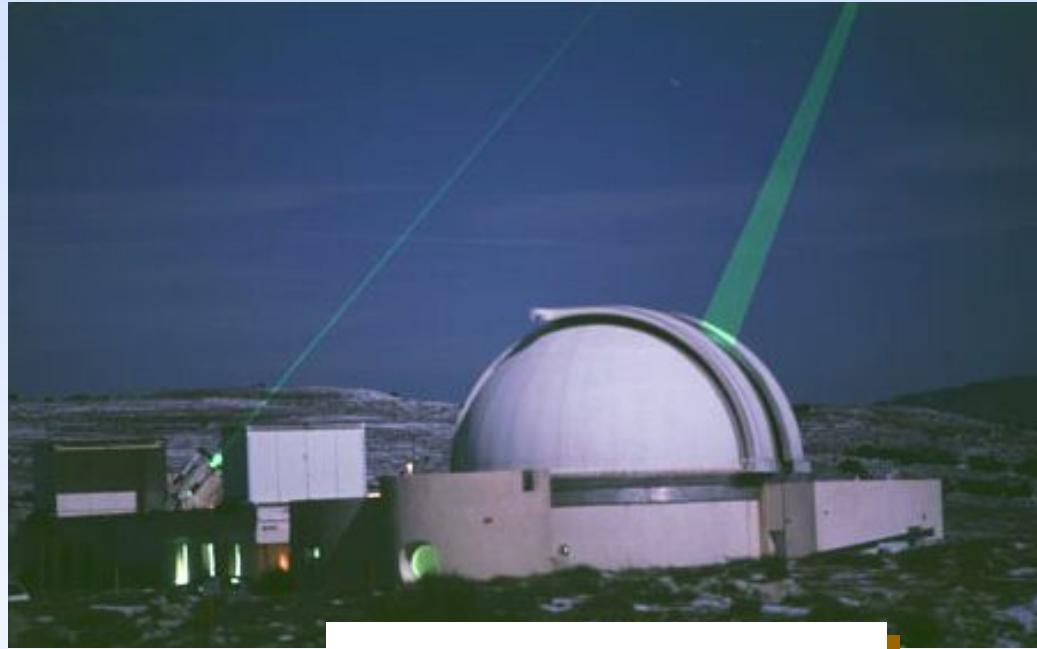
Torsion pendulum and attractor used in the short-range experiments



Pendulum, containing about a mole of polarized electrons, used to search for spin-coupled forces

# EP Test by Moon Laser Telemetry

From Mercury perihelion advance to :



## Parameters of the experiment

- Laser pulse 100ps
- 1 photon back out of  $10^{20}$  emitted
- 1 photon back every 100 pulses

## Results

Post-Newtonian parameters:

$$\beta - 1 = -0.001 \pm 0.004$$

$$\gamma - 1 = 0.002 \pm 0.004$$

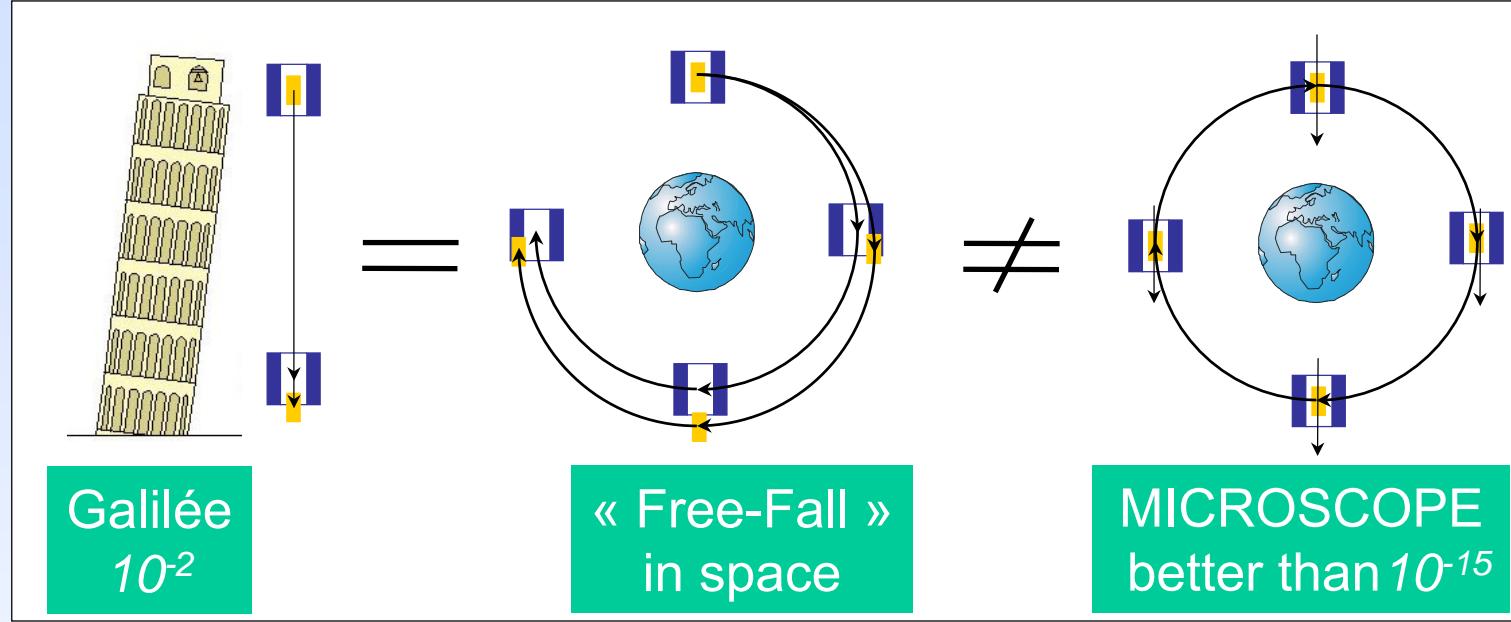
- EP test from 20 years measurements:

$$\delta = \left[ \frac{M_G}{M_I} \right]_{Earth} - \left[ \frac{M_G}{M_I} \right]_{Moon} = (-1 \pm 2) \times 10^{-13}$$

- Expected accuracy in 2010:  $5 \times 10^{-14}$



## Testing EP in space



**Space Laboratory = S/C in orbital motion, “quite” in free fall**

- Drag free system and fine attitude control demanded
- S/C : to protect from radiation pressures and residual drag the masses & to carry the measuring device and facilities

**Difference of orbital trajectory :**

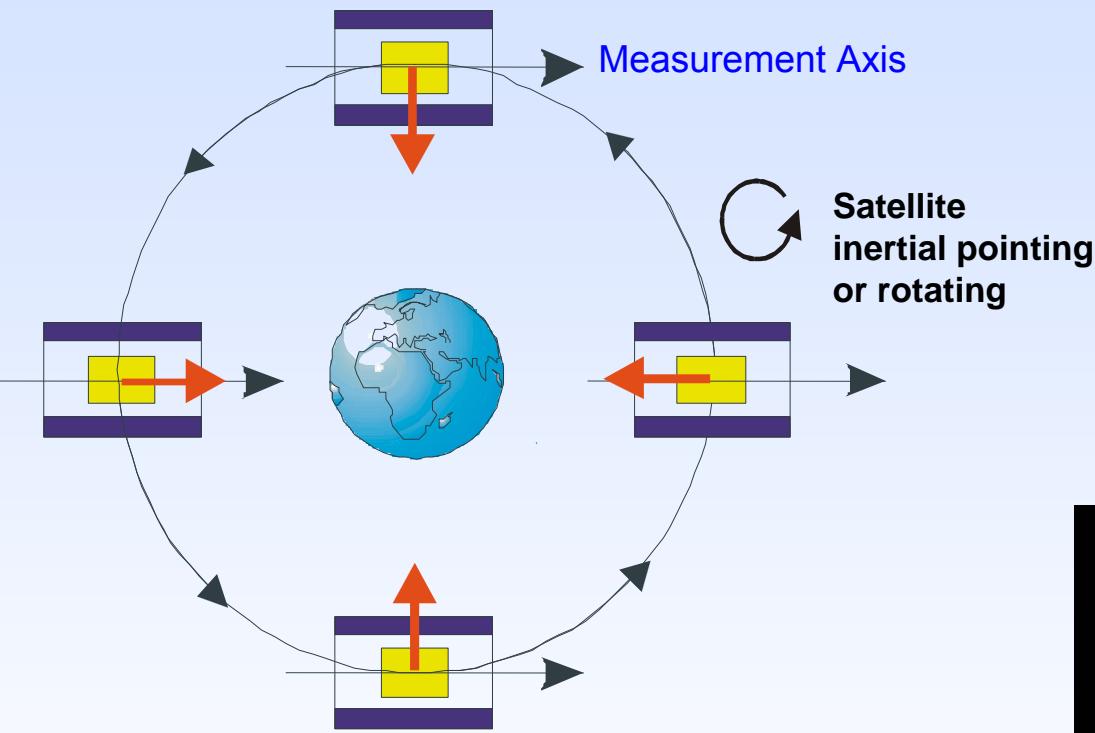
- Measured by ultrasensitive detectors (SQUIDS, capacitive, optical ...)
- Necessary « weak » springs to S/C (electrostatic, magnetic, mechanic)
- Non steady configuration

**Difference of necessary force to equalize the trajectories**

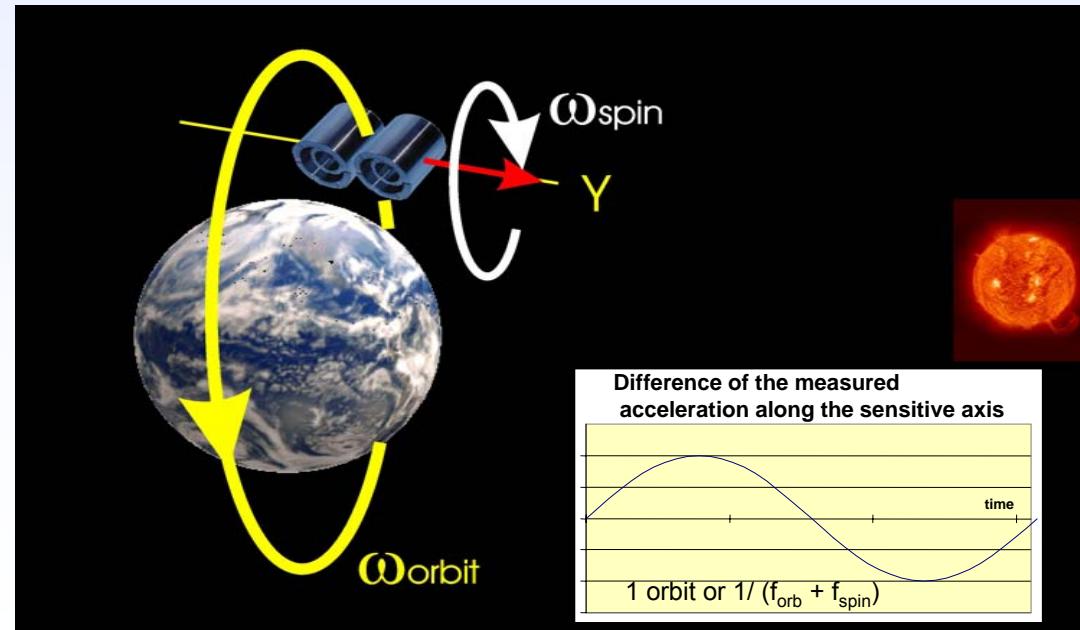
- Electrostatic servo-controlled system to maintain motionless the masses
- Stable and symmetric configuration => defect of symmetry = EP violation



# Equivalence Principle Test in Space



- Gravitational Source : The Earth
- Inertial Acceleration : Orbital Motion
- Control of the 2 masses on the same orbit with electrostatic pressure ( $< 10^{-11}\text{m}$ )
- Test duration : not limited by free-fall duration ( $> n$  times 20 orbits  $\sim 1.2 \cdot 10^5\text{s}$ )
- Spatial environment : reduced or controlled disturbances, drag free satellite
- Signal to be detected : well known phase and frequency signal





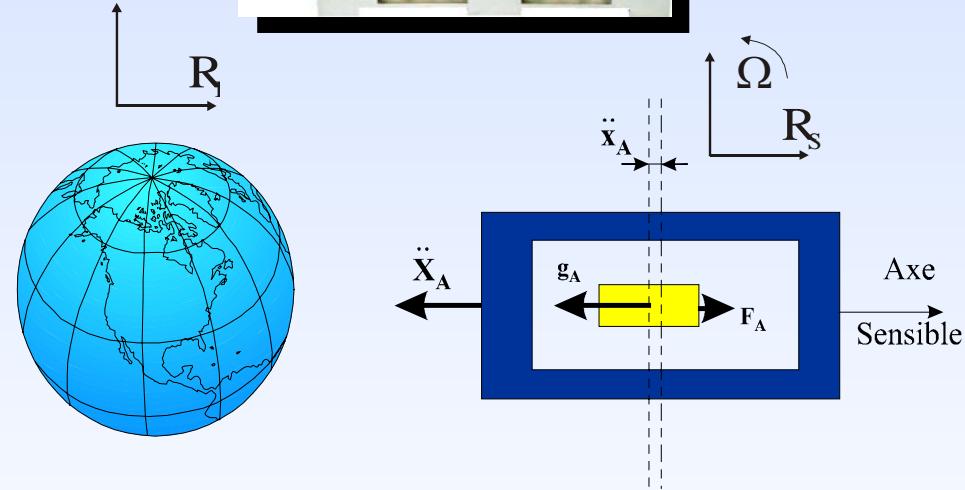
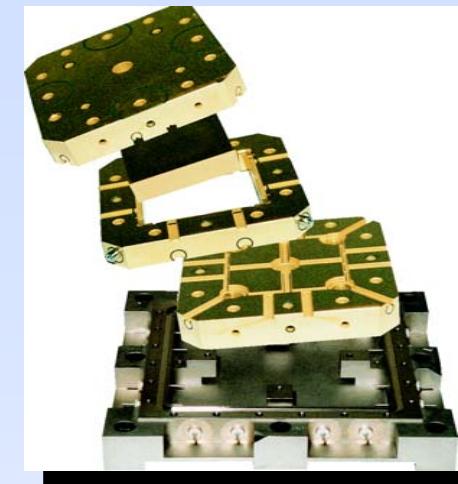
## MICROSCOPE APPROACH

- Opportunity of Micro satellite (100- 200 kg) mission
- Necessity of limited development & cost

**Payload case : < 40 kg, 40 W  
Room temperature operation**

**Take advantage of existing space  
electrostatic accelerometers :  
configuration to be optimized**

**EP Test-mass = Cylindric Proof-mass of  
electrostatic inertial sensor**



One Differential accelerometer = 2 inertial sensors with 2 concentric test-masses

When the 2 masses have different composition = EP Test

When the 2 masses have same composition = Test accuracy verification



# EP Test Mission Principle

## Accelerometer A Output:

$$\frac{\hat{F}_A}{m_{I_A}} = (I + K_A) F_A + E(F_A) + E_{n_A}$$

Difference of 2 inertial sensor measurements:

$$\frac{\hat{F}_A}{m_{I_A}} - \frac{\hat{F}_B}{m_{I_B}} \approx (K_A - K_B) \frac{\ddot{X}_A + \ddot{X}_B}{2}$$

$$+ \left( \overset{\circ}{X}_A + \overset{\circ}{x}_A - \overset{\circ}{X}_B - \overset{\circ}{x}_B \right) + 2\Omega \left( \overset{\circ}{X}_A + \overset{\circ}{x}_A - \overset{\circ}{X}_B - \overset{\circ}{x}_B \right)$$

$$+ (\Omega \times \Omega + \dot{\Omega}) (X_A + x_A - X_B - x_B)$$

$$- \left( \frac{m g_A}{m_{I_A}} + \frac{m g_B}{m_{I_B}} \right) \left( \frac{g_A - g_B}{2} \right) \left( I + \frac{K_A + K_B}{2} \right)$$

$$+ \left( \frac{F_{p_A}}{m_{I_A}} - \frac{F_{p_B}}{m_{I_B}} \right)$$

$$+ \left( \frac{m g_A}{m_{I_A}} - \frac{m g_B}{m_{I_B}} \right) \left( \frac{g_A + g_B}{2} \right) \left( I + \frac{K_A + K_B}{2} \right)$$

$$+ E(F_A) - E(F_B) + E_{n_A} - E_{n_B}$$

- (1) Common mode acceleration**

Scale factor matching  $\sim 3 \times 10^{-4}$ , Satellite drag-free control  $3 \times 10^{-10} \text{ ms}^{-2} \text{ Hz}^{-1/2}$   
Instrument structure stability (silica), Thermal control

- (2) Proof-mass relative motion**

structure stability & electrostatic control

Servo-loop control : electronics performance,  
Structural & Thermal Stability, Attitude Control

- (3) Satellite attitude motion**

Attitude control / proof-mass positioning  $20 \mu\text{m} \Rightarrow 0.1 \mu\text{m}$

- (4) Difference of Gravity field effects**

S/C stiffness and thermo-elastic behavior, Earth gravity gradient filtered out

- (5) Non gravitational acceleration**

Mass motion disturbances & forces on the mass,  
Actuator noise & sensing back-action

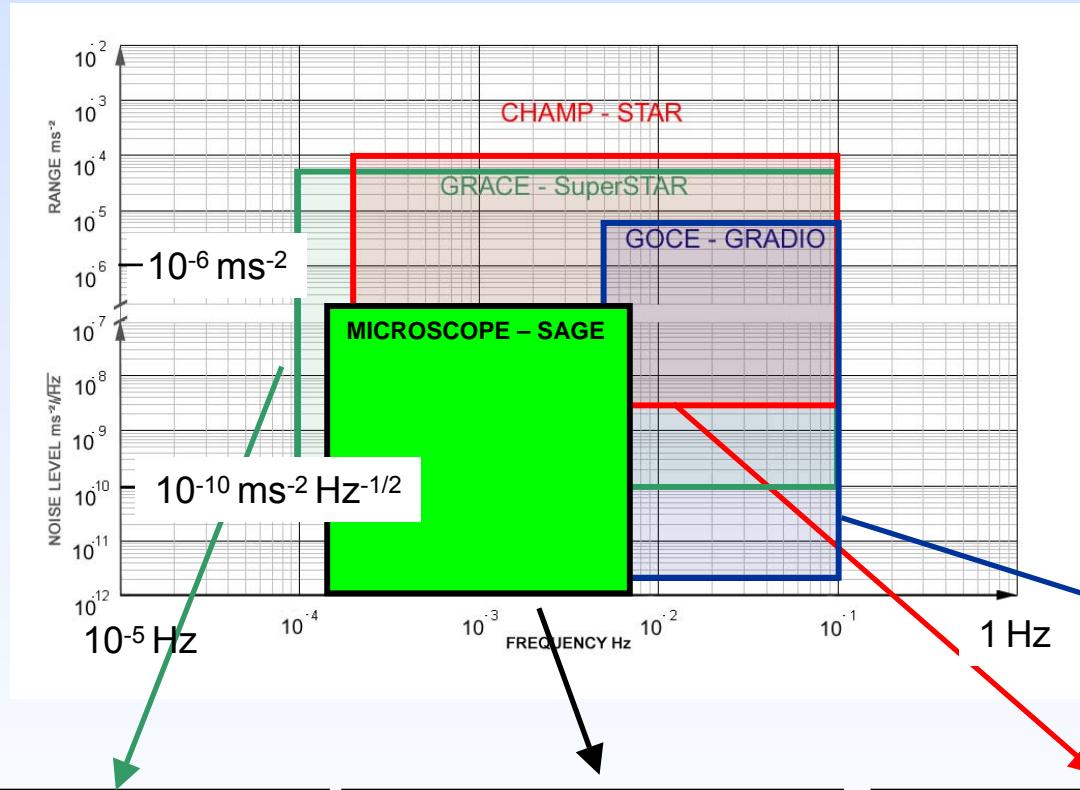
- Signal representative of EP violation**

- (6) Instrument (non-linearity & noise)**

Non linearity & Measurement electronics noise



# Differences between Accelerometers from STAR, SuperSTAR, GRADIO to SAGE



- $\Gamma_n : 3 \cdot 10^{-9} \text{ ms}^{-2}/\text{Hz}^{1/2}$
- $\Gamma_{\max} : 10^{-4} \text{ ms}^{-2}$
- $[2 \cdot 10^{-4}; 10^{-1}] \text{ Hz}$

- $\Gamma_n : 10^{-12} \text{ ms}^{-2}/\text{Hz}^{1/2}$
- $\Gamma_{\max} : 2.5 \cdot 10^{-7} \text{ ms}^{-2}$
- $[10^{-4}; 5 \cdot 10^{-3}] \text{ Hz}$

- $\Gamma_n : 10^{-10} \text{ ms}^{-2}/\text{Hz}^{1/2}$
- $\Gamma_{\max} : 5 \cdot 10^{-5} \text{ ms}^{-2}$
- $[10^{-4}; 10^{-1}] \text{ Hz}$

## SAGE Space Accelerometer for Gravitation Experience

Same concept & technology but

- Optimised core design
- Digital control loop
- Better control of the environment
- Frequency bandwidth



## GOCE Gradiometer

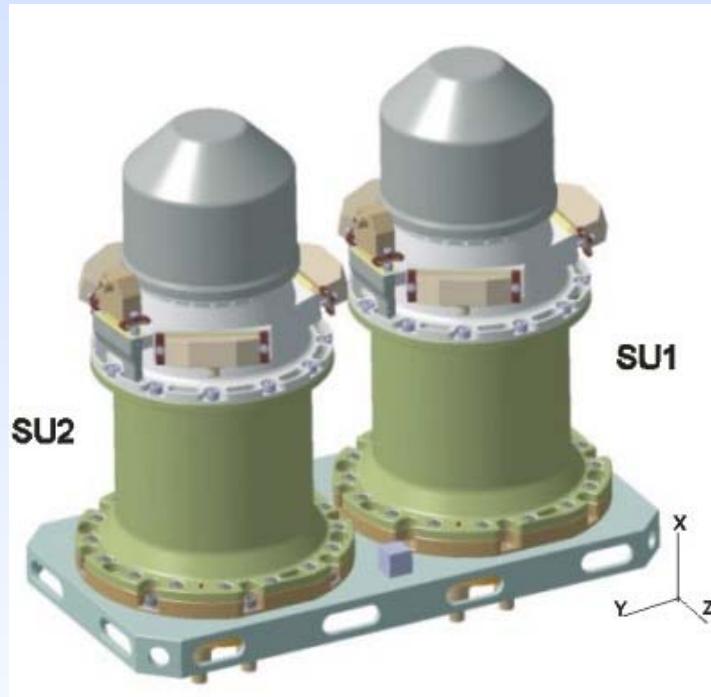


**STM GRADIOMETER**

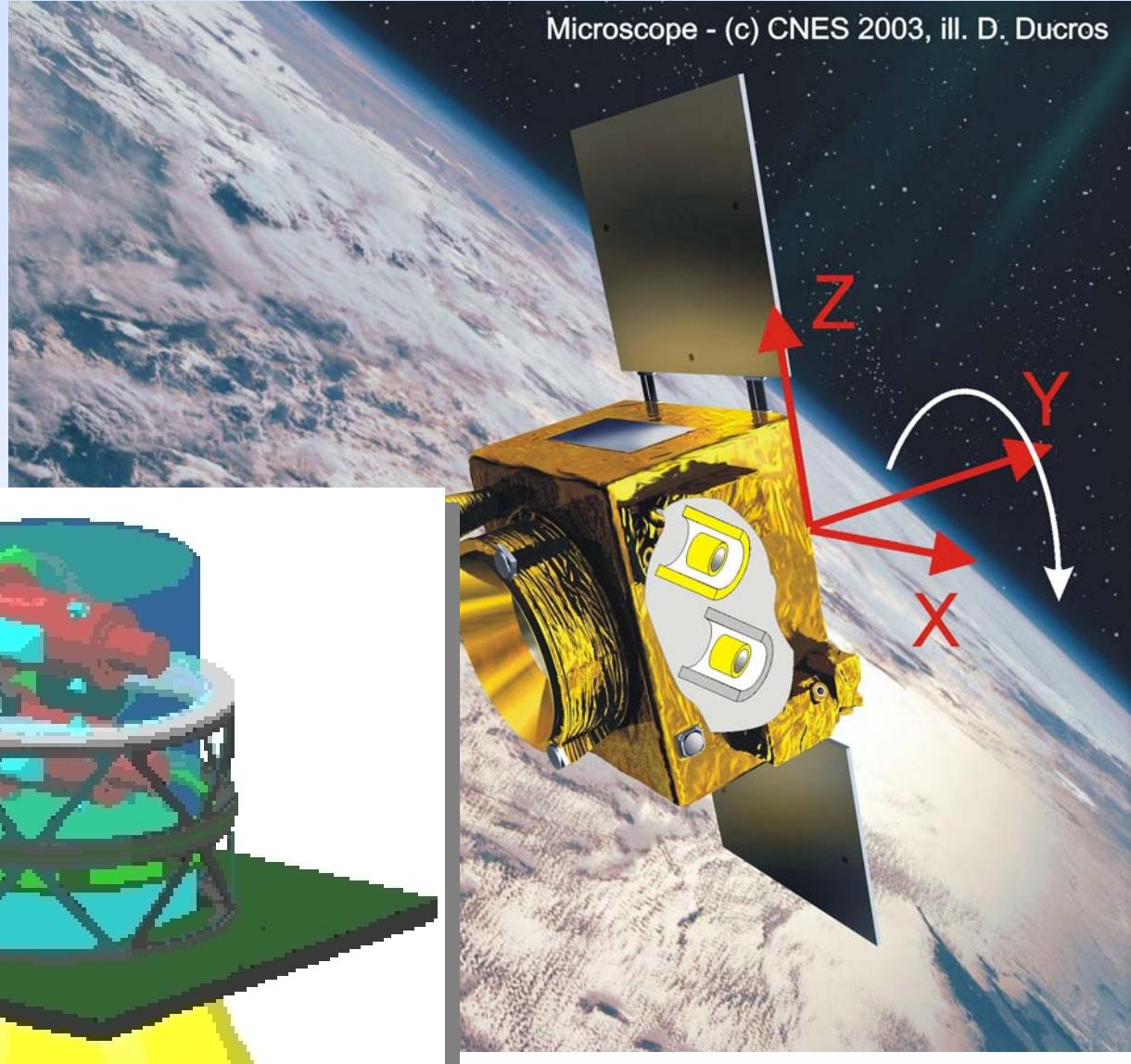




## MICROSCOPE PAYLOAD



2 similar differential  
accelerometers



# THERMAL Environment to be provided by the S/C

## Thermal specifications :

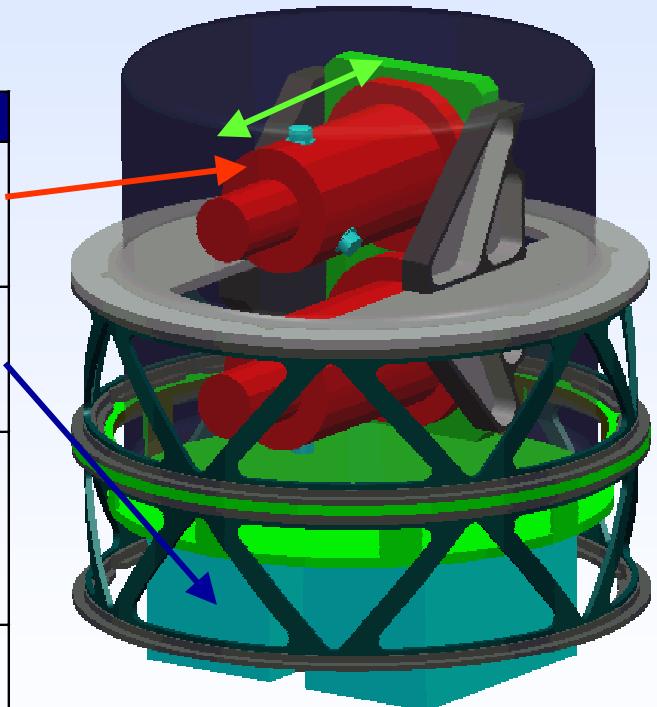
**Sensor (SU) Core thermal behavior**

**Parasitic forces (Radiometer effect, Radiation pressure, bias fluctuation)**

**Sensor Electronics (FEEU) sensitivity**

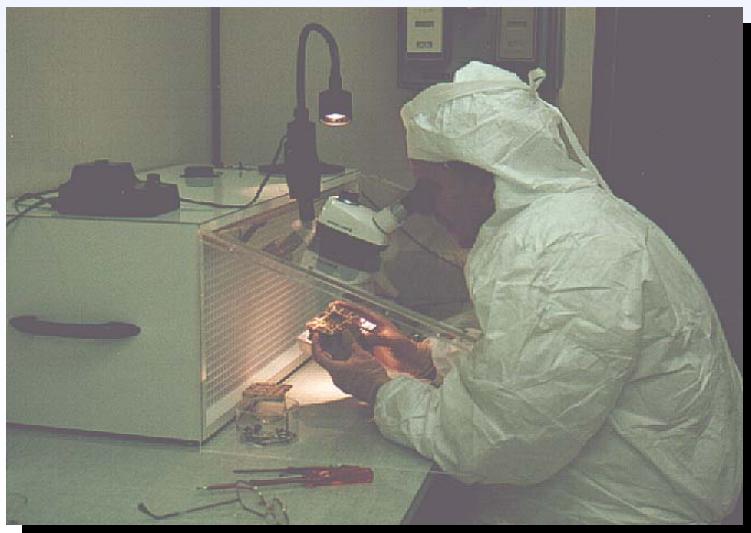
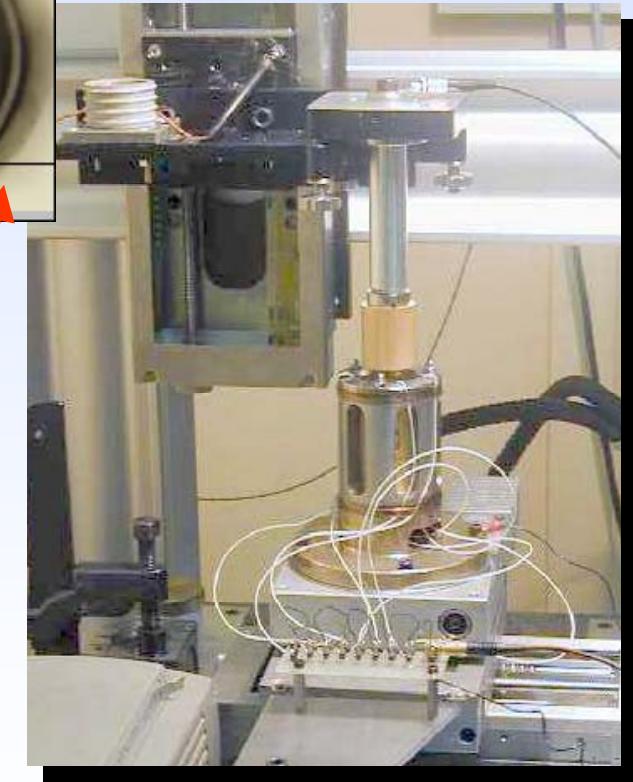
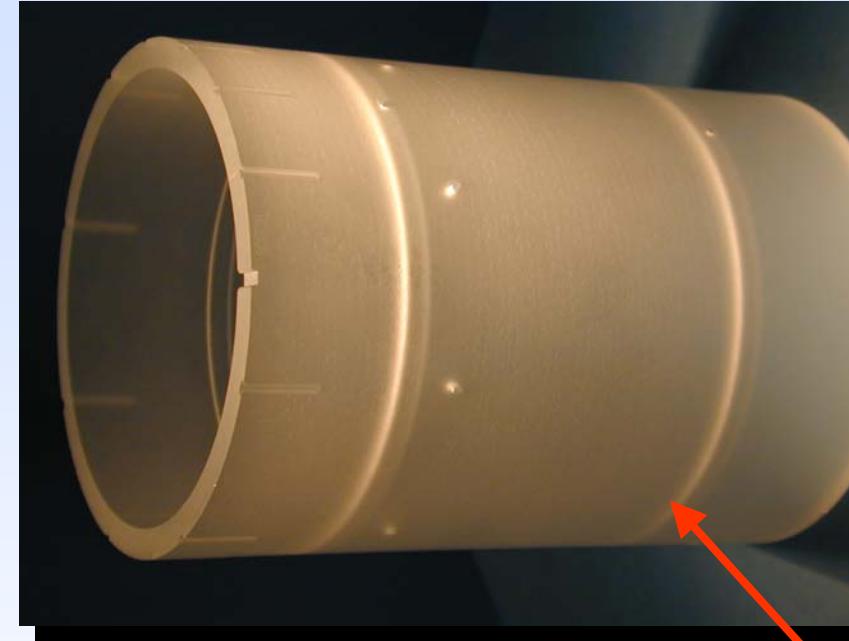
**Sensor interface electronics (ICU) sensitivity**

Location	Value
On SU skin	<ul style="list-style-type: none"> <li>- <math>0.3 \text{K Hz}^{-1/2}</math> between 0.1mHz and 0.1Hz</li> <li>- 1 mK @ fep</li> <li>- 10 mK @ 2 fep et 4 fep</li> </ul>
On FEEU skin	<ul style="list-style-type: none"> <li>- <math>3 \text{K Hz}^{-1/2}</math> between 0.1mHz and 0.1Hz</li> <li>- 10 mK @ fep</li> <li>- 100 mK @ 2 fep et 4fep</li> </ul>
Thermal gradients on SU (axial)	<ul style="list-style-type: none"> <li>- 1K/m at DC</li> <li>- <math>3 \text{ K/m Hz}^{-1/2}</math> between 0.1mHz and 0.1Hz</li> <li>- 10 mK/m @ fep</li> <li>- 100 mK/m @ 2 fep et 4 fep</li> </ul>
At ICU interface	<ul style="list-style-type: none"> <li>- <math>10 \text{ K Hz}^{-1/2}</math> between 0.1mHz and 0.1Hz</li> <li>- 2.5 K @ fep</li> </ul>



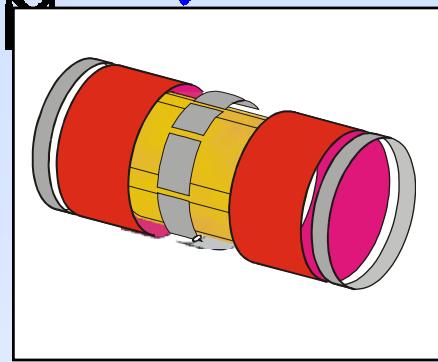


## Sensor Core

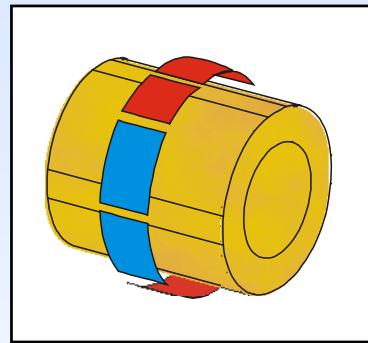


- Low CTE material : Silica
- Ultrasonic machining
- Gold coating (sputtering)
- Accurate metrology
- Clean room integration
- micromys, arcsecond

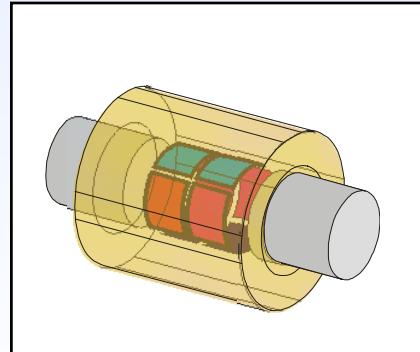
# Electrostatic Inertial Sensor Configuration



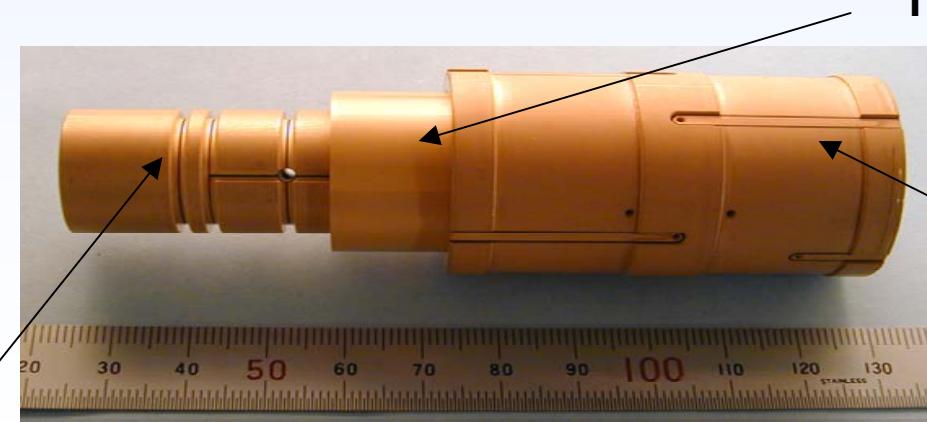
Axial electrodes



Spin electrodes



Radial electrodes



Test-mass

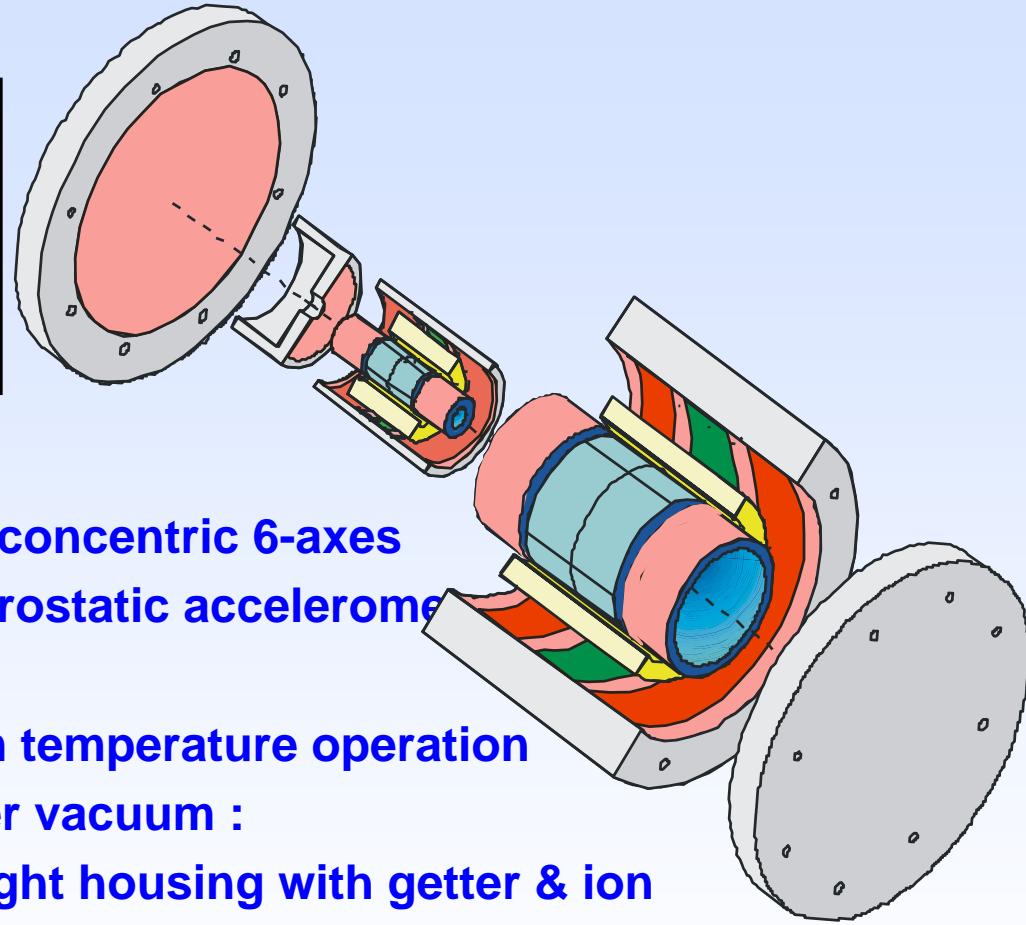
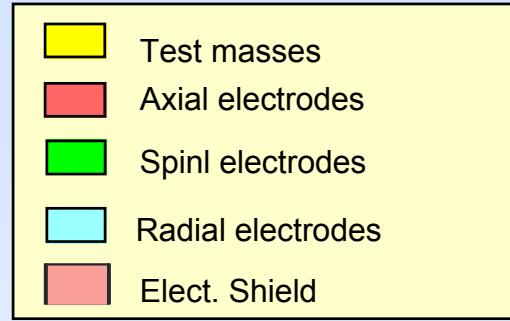
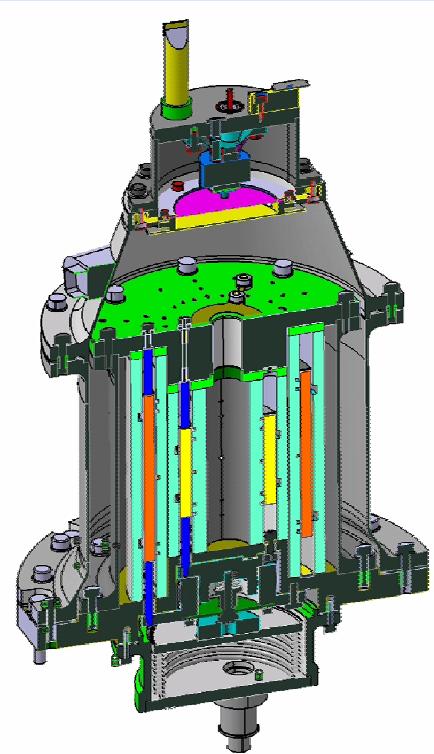
EP  
Test data

External electrode cylinder

Internal electrode cylinder



## SAGE instrument : Differential Accelerometer Core Configuration



- Two concentric 6-axes electrostatic accelerometers
- room temperature operation
- under vacuum :
- --> tight housing with getter & ion blocking mechanism for launch
- specific alignment and positionning rods



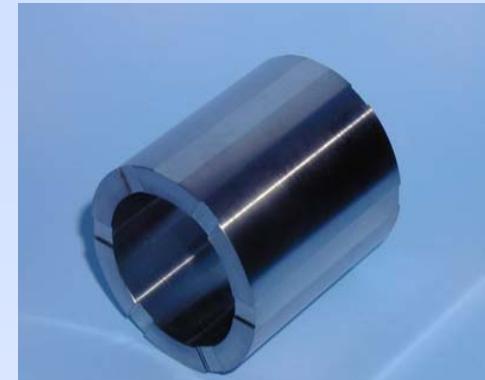
# Material selection

On the basis of an eventual violation dependency on:

- E/M T. Damour et al. (2002)
- With  $E = Z(Z-1)/(N+Z)^{1/3}$  &  $M = m/u$
- (atomic mass m and  $u = 931.49432 \text{ MeV}$ )

Mat i	Mat j	$(E/M)_i - (E/M)_j$
Pt	Ti	2.67
Pt	Cu	2.11
Pt	Pt	0 (whatever the mass)

Pt/Ti larger signal but lower instrument resolution



**PTB (Braunschweig)  
machining of titanium alloy mass**

**R<sub>a</sub> = 0.2 μm**

**Flat areas C, D, E, F**

- Planeity < 0.5μm
- Perpendicularity 2 by 2 < 4 arc sec
- Parallelism / dG < 4 arc sec
- Parallelism 2 by 2 < 4 arc sec

	B mean	Z	M mean	ρ (kg m <sup>-3</sup> )	χ(CGS)10 <sup>-6</sup>	CTE (K <sup>-1</sup> )	λ (W/m/K)
Pt	195.11626	78	193.56593	21.45	1.1	9.1 10 <sup>-6</sup>	71.6
Ti	47.93050	22	47.50717	4.5	3.43	8.5 10 <sup>-6</sup>	21.6
Cu	62.61652	29	63.05216	8.96	-0.086	16.4 10 <sup>-6</sup>	401



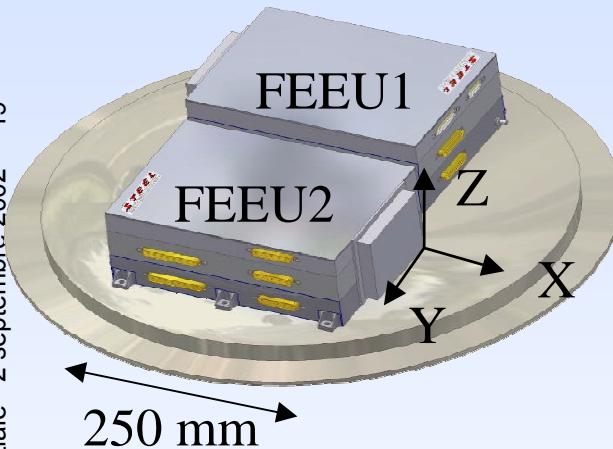
re 2002 - 18





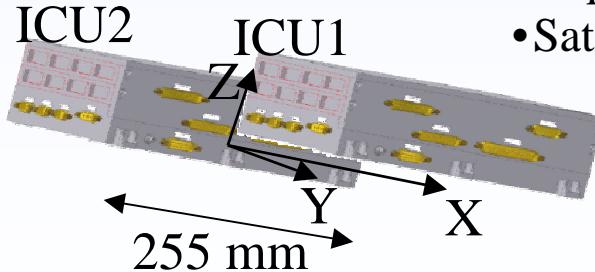
# Instrument Components

## Front End Electronics Unit

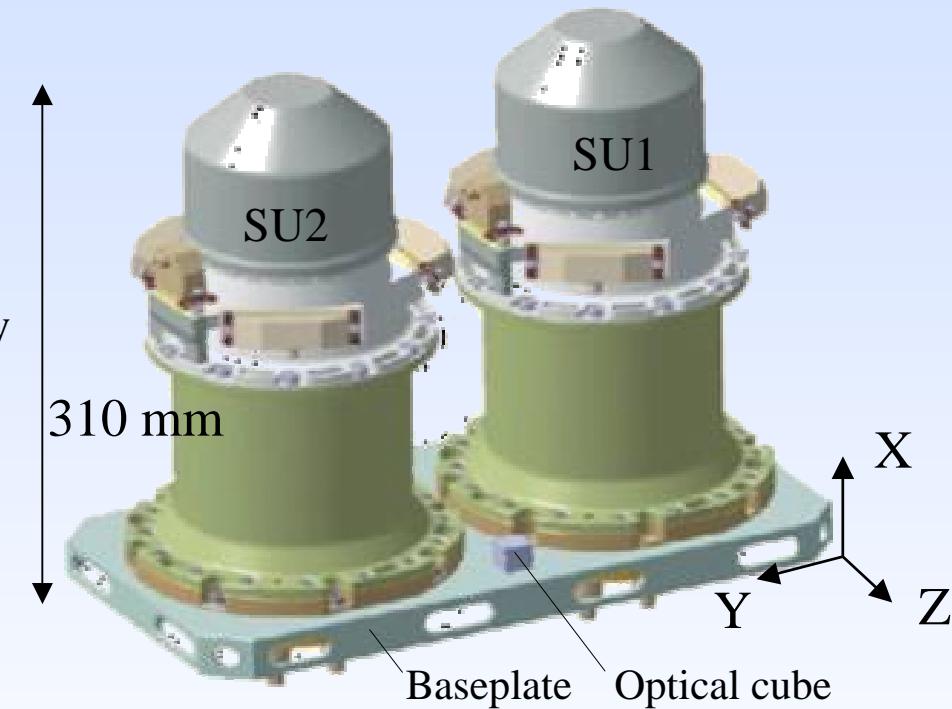


- Low noise electronics
  - Capacitive detectors
  - DACs/ADCs
- Requires temperature stability

## Interface Control Unit



- SU operation
- Experiment control
- Satellite interface



## Sensor Unit

- Low power operation
- Requires precise alignment with star camera



# Instrument resolution

## Test-mass motion disturbances

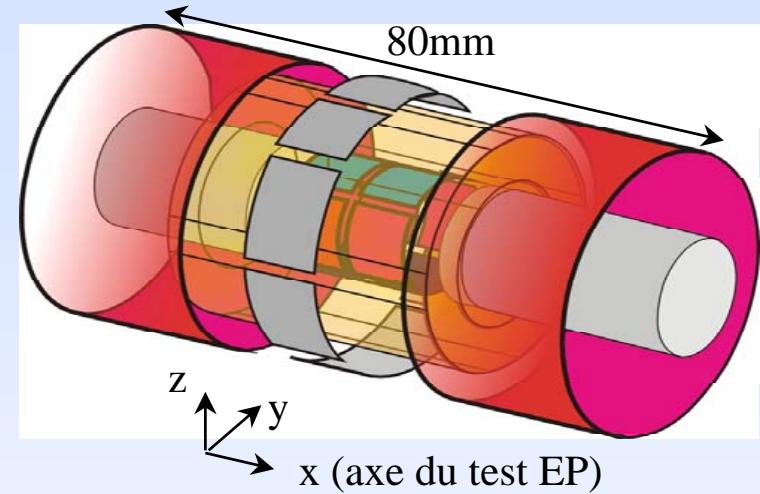
- Stiffnesses
- Damping
- Bias force fluctuations:
  - electrical & magnetic
  - residual gas
  - radiation pressure
  - gravitational

## Electrostatic loop Noise

- Capacitive position sensing
- Electrostatic actuators
- Pick-up measurement
- ⇒ Back Actions

## Thermal sensitivities

## Alignments & scale factor matching



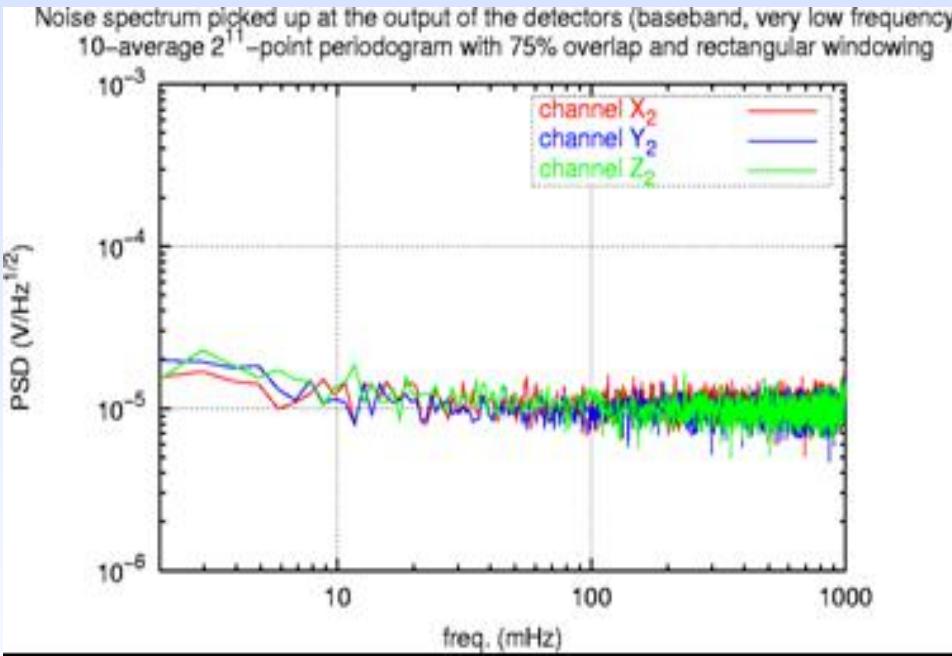
amplitude	X	Y/Z
Biais ( $K_0$ ) ( $m/s^2$ )	$0,54 \cdot 10^{-7}$	$8,0 \cdot 10^{-7}$
Fact d'échelle ( $K_I$ )	$1 \pm 10^{-2}$	$1 \pm 1 \cdot 10^{-2}$
Alignements ( $\alpha, \beta, \gamma$ )	$\pm 10^{-2}$	$\pm 10^{-3}$
Couplages ( $\varepsilon, \eta, \mu$ )	$\pm 10^{-4}$	$\pm 10^{-4}$
Résolution ( $\Gamma_n$ ) ( $m/s^2/\sqrt{Hz}$ )	$10^{-12}$	$8 \cdot 10^{-11}$



# Analog Electronics test results

Obtained with Electronics realised for LISA Pathfinder inertial sensor

- Capacitive position sensor noise



$10^{-19} \text{ F}/\text{Hz}^{1/2}$  (**Sensitivity**  $\sim 20\text{V}/\text{pF}$ )

corresponding to :

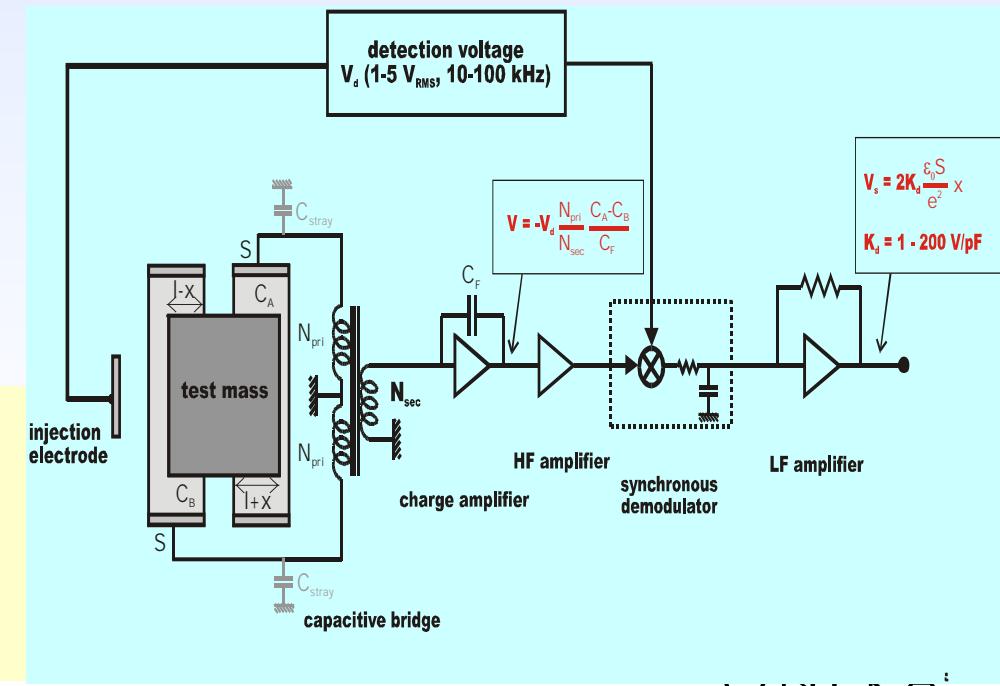
-  $10^{-9} \text{ m}/\text{Hz}^{1/2}$  @ 4 mm

LTP configuration with large gaps

-  $10^{-10} \text{ m}/\text{Hz}^{1/2}$  @ 400  $\mu\text{m}$

MICROSCOPE configuration

leading to at least  $3 \cdot 10^{-12} \text{ m}$  @  $f_{EP}$

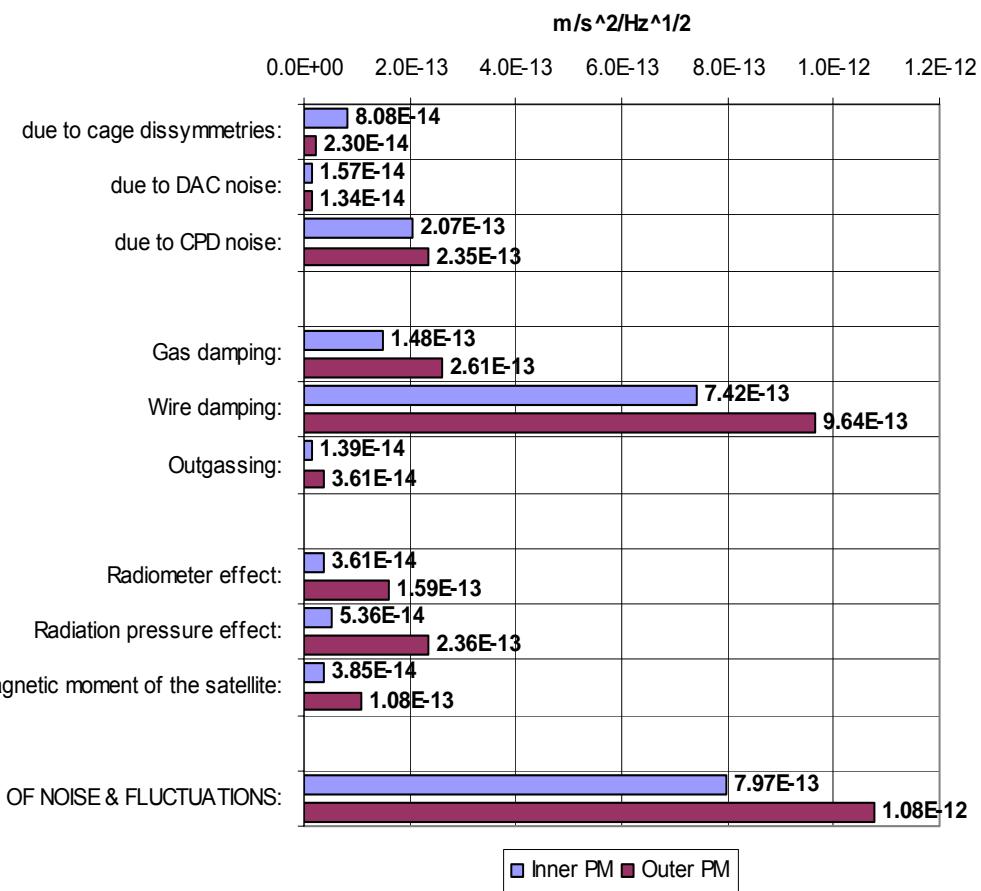
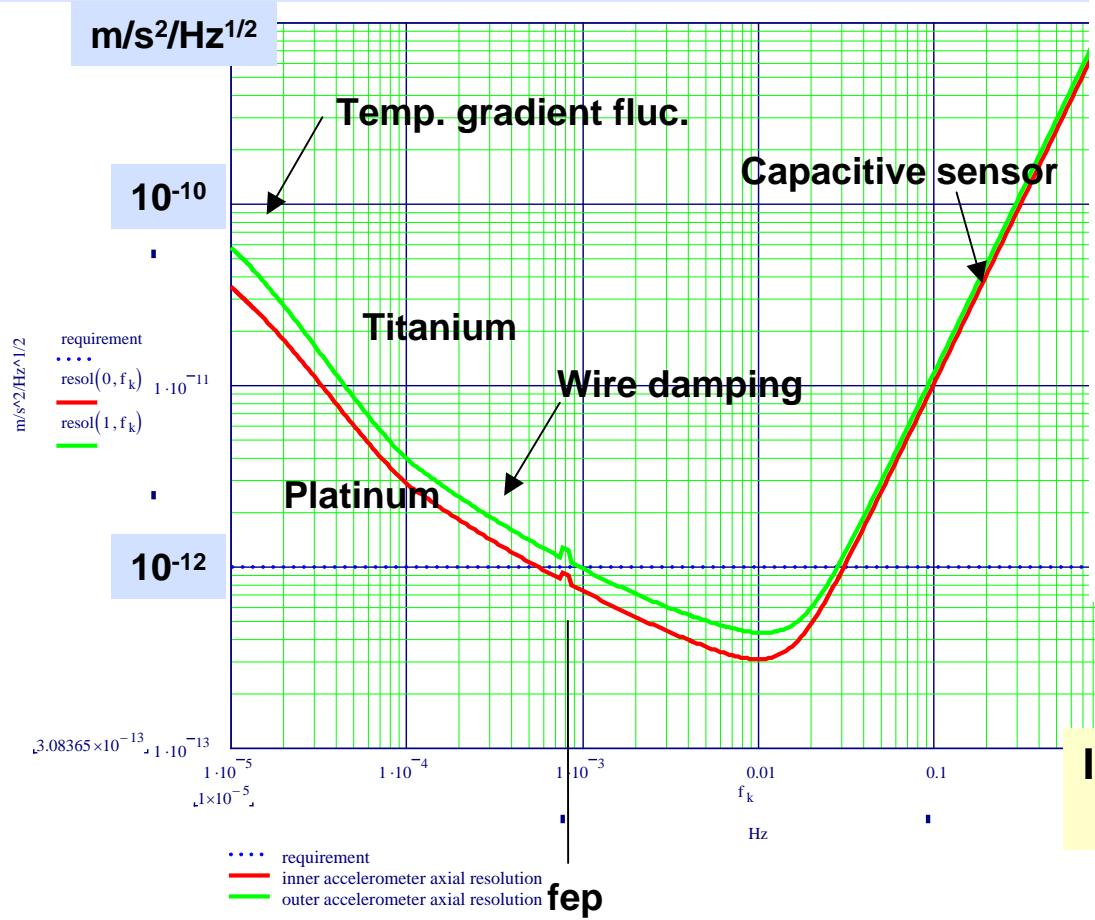


## Electrostatic actuator noise :

- Drive Voltage Amplifier noise :  $100 \text{ nV}/\text{Hz}^{1/2}$   
(input noise with Amp. gain 16)
- Corresponding to :  $10^{-10} \text{ N}/\text{Hz}^{1/2}$  to  $10^{-13} \text{ N}/\text{Hz}^{1/2}$   
according to accelerometer conf. and axis



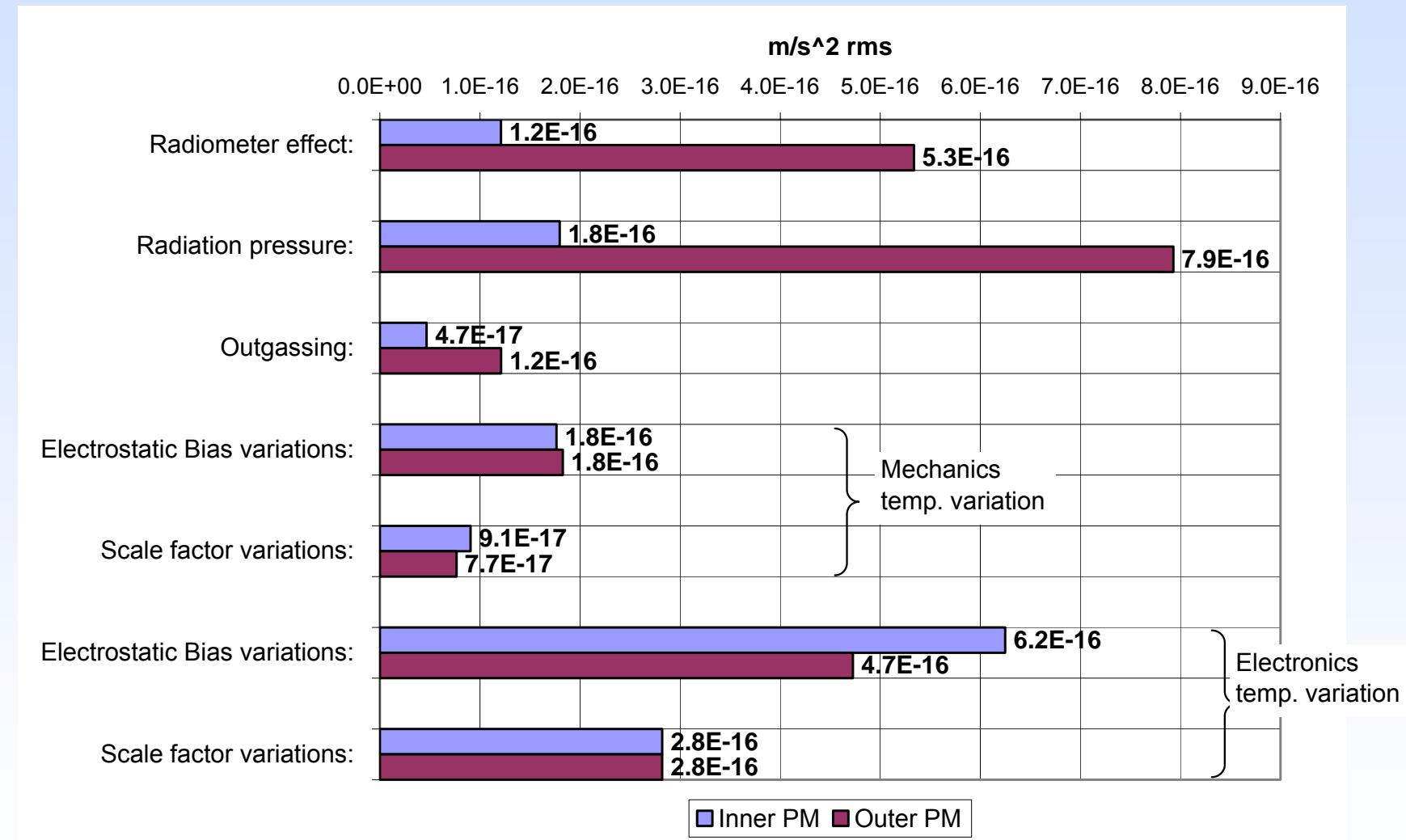
# Random noise



In agreement with 10<sup>-15</sup> EP test accuracy  
(20 orbits integration period)



## Systematic Errors



**Quadratic sum ~ 1.5 E-15 (non correlated source and distributed phase)**



## Instrument Calibration : sensitivity matrix

$$\begin{pmatrix} \Gamma_{mes,x} \\ \Gamma_{mes,y} \\ \Gamma_{mes,z} \end{pmatrix} \approx \begin{pmatrix} K_{0,x} \\ K_{0,y} \\ K_{0,z} \end{pmatrix} + \begin{pmatrix} K_{1x} & \varepsilon + \theta_z & \eta - \theta_y \\ \varepsilon - \theta_z & K_{1y} & \mu + \theta_x \\ \eta + \theta_y & \mu - \theta_x & K_{1z} \end{pmatrix} \cdot \begin{pmatrix} \Gamma_{réel,x} \\ \Gamma_{réel,y} \\ \Gamma_{réel,z} \end{pmatrix} + \begin{pmatrix} \Gamma_{n,x} \\ \Gamma_{n,y} \\ \Gamma_{n,z} \end{pmatrix}$$

One Inertial Sensor  
Linear Model

Measure	Bias	Sensitivity Matrix	Actual Mass Acc.	Noise
---------	------	--------------------	------------------	-------

$$\Gamma_{mes,1} = K_{0,1} + M_1 \cdot \Gamma_{réel,1} + \Gamma_{n,1}$$

$$\Gamma_{mes,2} = K_{0,2} + M_2 \cdot \Gamma_{réel,2} + \Gamma_{n,2}$$

Instrument data  
outputs from 2 Sensors

Differential mode

$$\Gamma_{mes,diff} = \frac{\Gamma_{mes,1} - \Gamma_{mes,2}}{2}$$



$$\Gamma_{mes,diff} = K_{0,diff} + M_{com} \cdot \Gamma_{réel,diff} + M_{diff} \cdot \Gamma_{réel,com} + \Gamma_{n,diff}$$

Common mode

$$\Gamma_{mes,com} = \frac{\Gamma_{mes,1} + \Gamma_{mes,2}}{2}$$

$$\frac{\Gamma_{réel,1} - \Gamma_{réel,2}}{2} = \left( \frac{1}{2} \cdot \delta g + ([T] - [I]) \cdot \frac{\Delta}{2} \right)$$

$$\frac{\Gamma_{réel,1} + \Gamma_{réel,2}}{2} \approx \Gamma_{surface}$$

$$\delta = \left( \frac{m_{g1}}{m_{i1}} - \frac{m_{g2}}{m_{i2}} \right) \quad \Delta : 2 \text{ mass offcentring} \quad (< 20\mu\text{m})$$



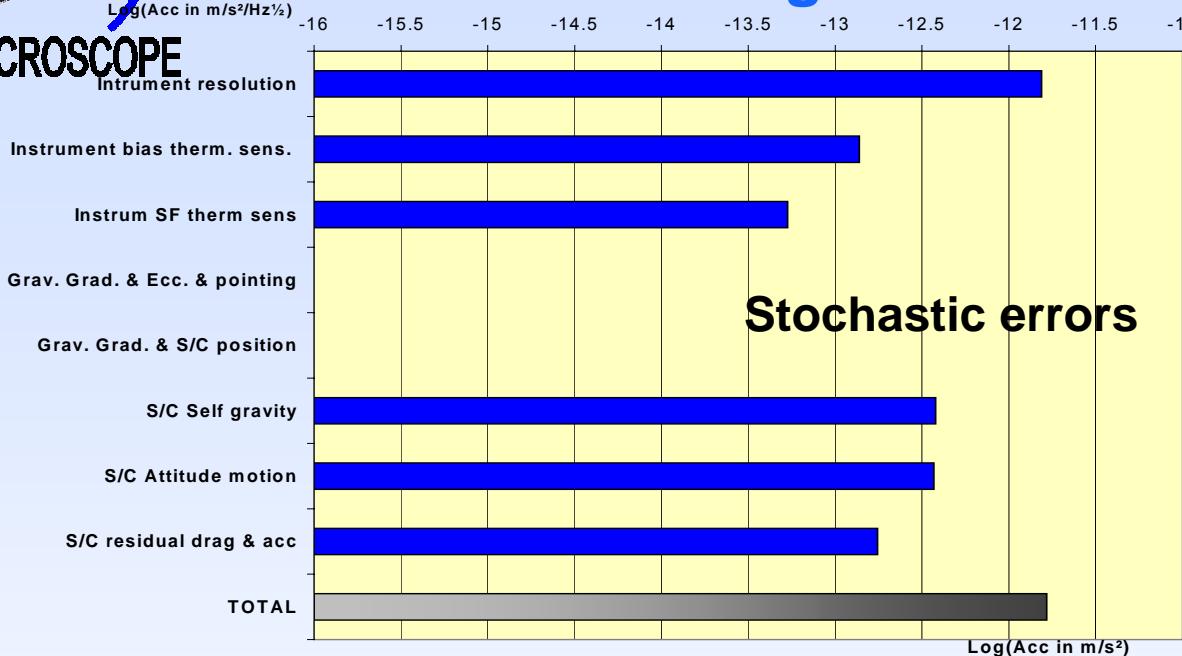
## Calibration: calibrated parameters (summary)

Parameters	Maximum value by construction	Impact before calibration	Spec for $e=5\cdot10^{-3}$	Impact after calibration
$\theta_{cy}$ and $\theta_{cz}$ for $\Delta \leq 20\mu\text{m}$	$1.5\cdot10^{-3} \text{ rad}$	$3.4\cdot10^{-16} \text{ m}\cdot\text{s}^{-2}$	$10^{-3} \text{ rad}$	$2.4\cdot10^{-16} \text{ m}\cdot\text{s}^{-2}$
$K_{cx}\cdot\Delta_x$ and $K_{cx}\cdot\Delta_z$ ( $K_{cx}\leq10^{-2} \text{ rad}$ )	$20,2 \mu\text{m}$	$8\cdot10^{-14} \text{ m}\cdot\text{s}^{-2}$	$0,1 \mu\text{m}$	$10^{-17} \text{ m}\cdot\text{s}^{-2}$
$\Delta_y$	$20 \mu\text{m}$	$3.4\cdot10^{-16} \text{ m}\cdot\text{s}^{-2}$	$0,4 \mu\text{m}$	$7\cdot10^{-18} \text{ m}\cdot\text{s}^{-2}$
$K_{dx}$	$10^{-2}$	$6\cdot10^{-13} \text{ m}\cdot\text{s}^{-2}$	$1,5\cdot10^{-4}$	$6\cdot10^{-17} \text{ m}\cdot\text{s}^{-2}$
$\theta_{dy}$ and $\theta_{dz}$	$10^{-3} \text{ rad}$	$1.2\cdot10^{-12} \text{ m}\cdot\text{s}^{-2}$	$5\cdot10^{-5} \text{ rad}$	$1.2\cdot10^{-16} \text{ m}\cdot\text{s}^{-2}$

e: orbit excentricity in MICROSCOPE nominal configuration



# Mission Error Budget: in rotating mode



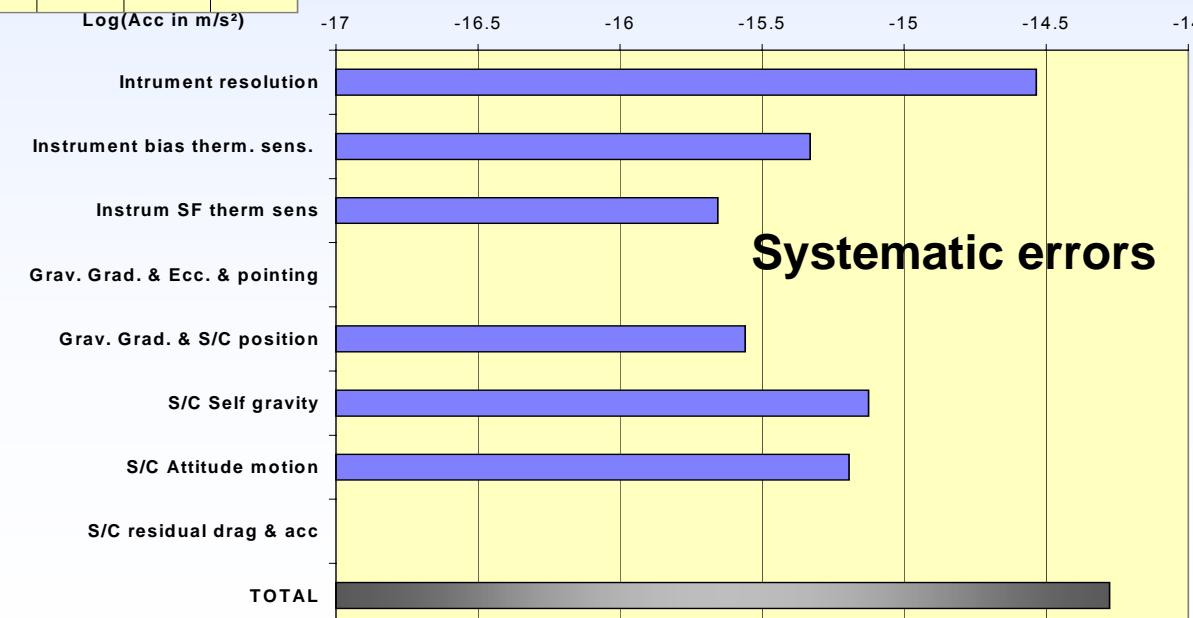
EP test @  $7.8 \cdot 10^{-4}$ Hz

Sensor limits :

$-1.7 \cdot 10^{-12} \text{ ms}^{-2} \text{ Hz}^{-1/2}$

$-4.7 \cdot 10^{-15} \text{ ms}^{-2}$  when direct sum of any source tone disturbance  
( $1.5 \cdot 10^{-15} \text{ ms}^{-2}$  when quadratic sum, rejection in the difference : ?)

Mission minimum performance :  $6.9 \cdot 10^{-15} \text{ ms}^{-2}$



EP TEST  $0.9 \times 10^{-15}$



## MICROSCOPE : PLANNING

- nov. 03: Phase A Review : Mission & Satellite
- jan. 04 - juin 04 : Phase B1, Review successful on 17/06/04
- juin 04 - avr. 05 : Phase B2, --> Preliminar Definition Review
- mai 05 - juin 06 : Phase C, --> Critical Definition Review
- mars 06 - mars 07: Phase D Instrument, --> Test & Acceptance Review for integ.
- juil. 07 - déc.07 : Satellite Intégration, --> Flight Acceptance Review

**Launch in March 08**

