

Constraining asteroid dynamical models using GAIA data

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In short...

- GAIA will provide extremely accurate orbits and spin information-solutions for a large number of asteroids.
- Combining with data (albedo, size) from other missions, we will have a complete physical/orbital picture for a large set of objects.

→ We could test dynamical models of the interplay between gravitational perturbations (chaotic diffusion in e , i) and Yarkovsky/YORP forces (drift in a).

→ Of special interest are: (i) groups of resonant objects (e.g. 2/1, 7/3) and (ii) asteroid families, hosting a significant component of chaotic motion (e.g. Veritas).

- We need to be able to run **thousands** of simulations
 - to **match** an **observed distribution** and, using optimization techniques,
 - to **probe** the **Yarkovsky “law”** ($da/dt \sim f(D, \dots)$), the **initial ejection velocity field**, etc...

Transport in action space: a statistical model

- We have introduced the use of a random-walk approximation, that describes chaotic diffusion in the space of proper elements (actions), as a tool to study the evolution of (chaotic) asteroid families:
 - compute the transport (diffusion) coefficient $D(e,i)$ on a grid covering the neighborhood of a family/group of asteroids
 - use D in a simple random-walk model to study the motion of fictitious family members
 - match the observed distribution → get the *age* of the family!
 - Only a few seconds for each realization of a 10 My evolution!!
- Successfully applied to the *Veritas* family (Tsiganis et al. 2007) – result agrees with Nesvorny et al. 2003
- Novakovic et al (2010a,b) extended the model by introducing **evolution** in a due to **Yarkovsky** (also **YORP** included)
- Here we will use the same model for studying a larger region of the asteroid belt (a 3-D cube of initial conditions)

Initial conditions and computational procedure

- We plan to study the region between the 5/2 and 7/3 mean motion resonances in the asteroid belt:

$$2.82 \text{ AU} < a < 2.96 \text{ AU}$$

$$0 < e < 0.4$$

$$0 < i < 20 \text{ deg}$$

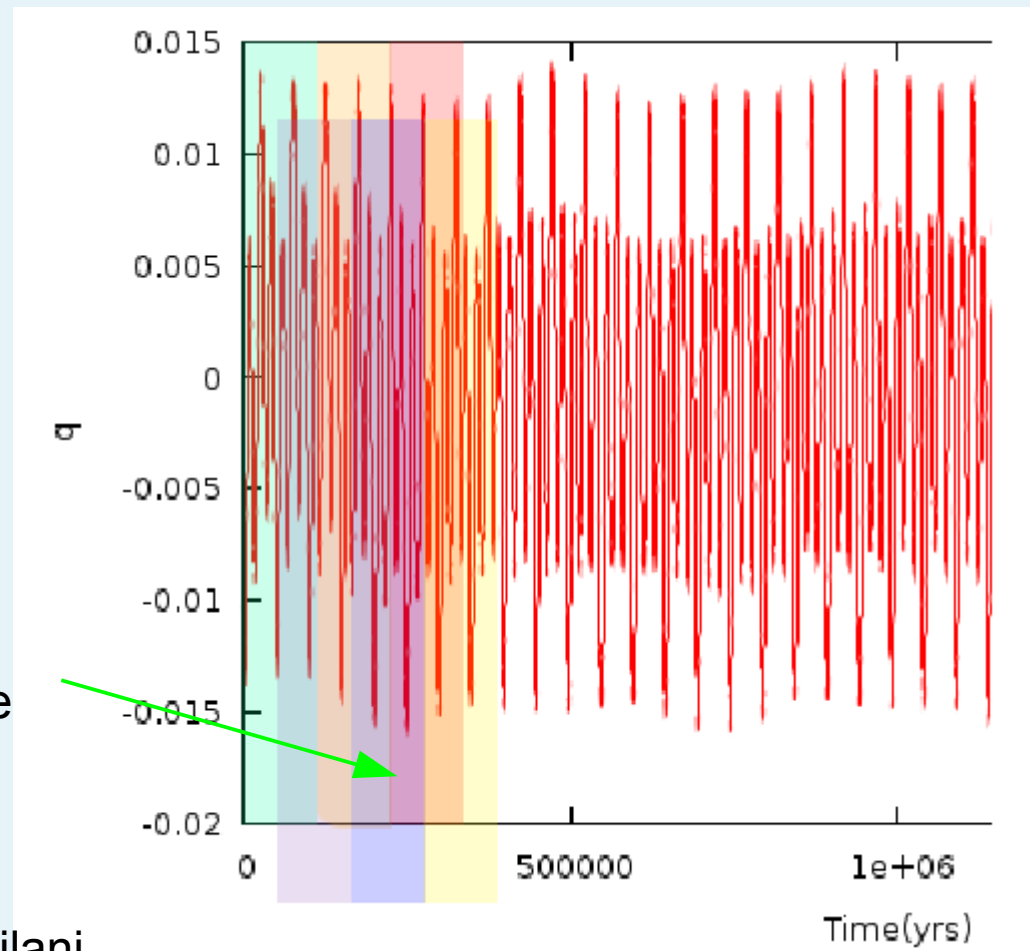
→ a sample of 100,000 orbits integrated for 2 My ! (a few days...)

→ only need to be done once!

- Each time-series is split into 'windows', and proper elements are computed in each window

→ time-series of e_p, I_p

as in the synthetic procedure of Milani & Knezevic

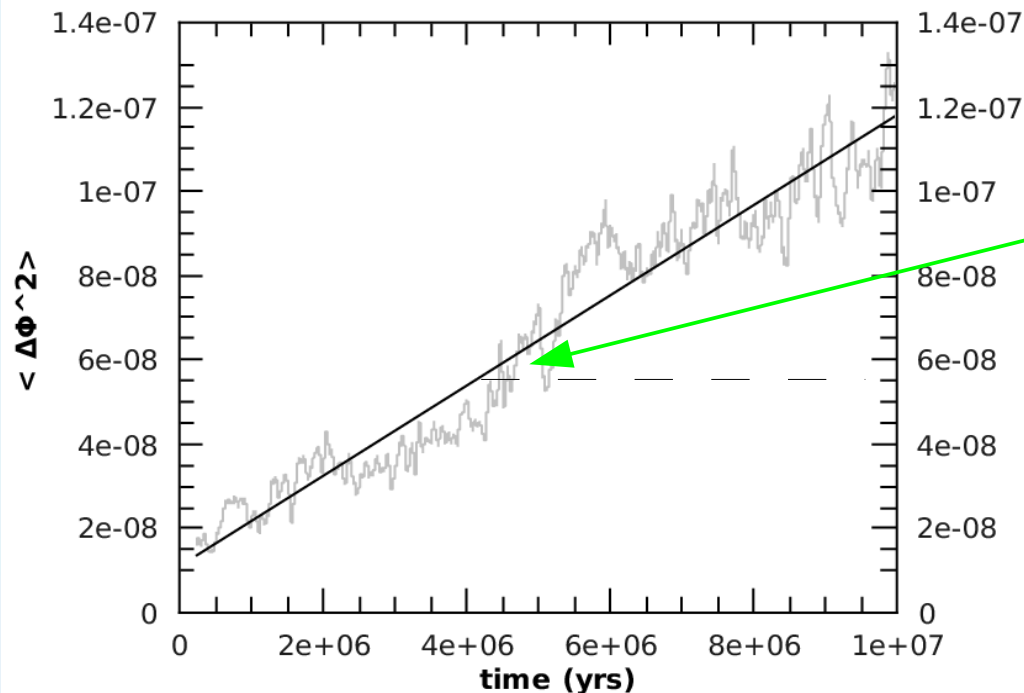
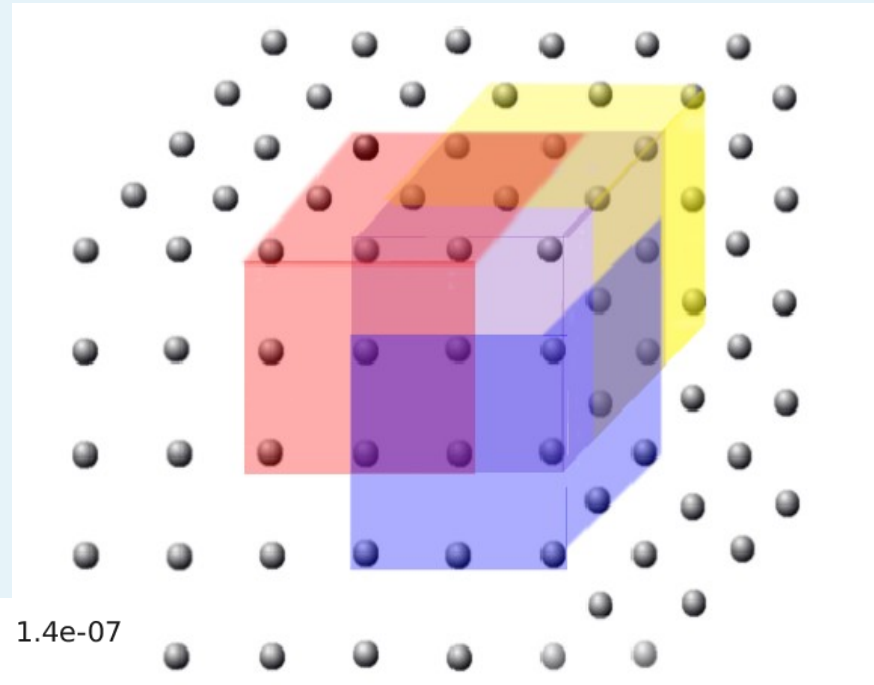


→ Group neighboring objects by ~30-100 and compute the **mean squared displacement** (msd) in each action as a function of time

$$\langle (\Delta \Phi_i)^2 \rangle = \langle [\Phi_i(t) - \Phi_i(0)]^2 \rangle_N$$

$$\Phi_i \sim X_i^2 \quad [X_i = e_p, \sin(i_p)]$$

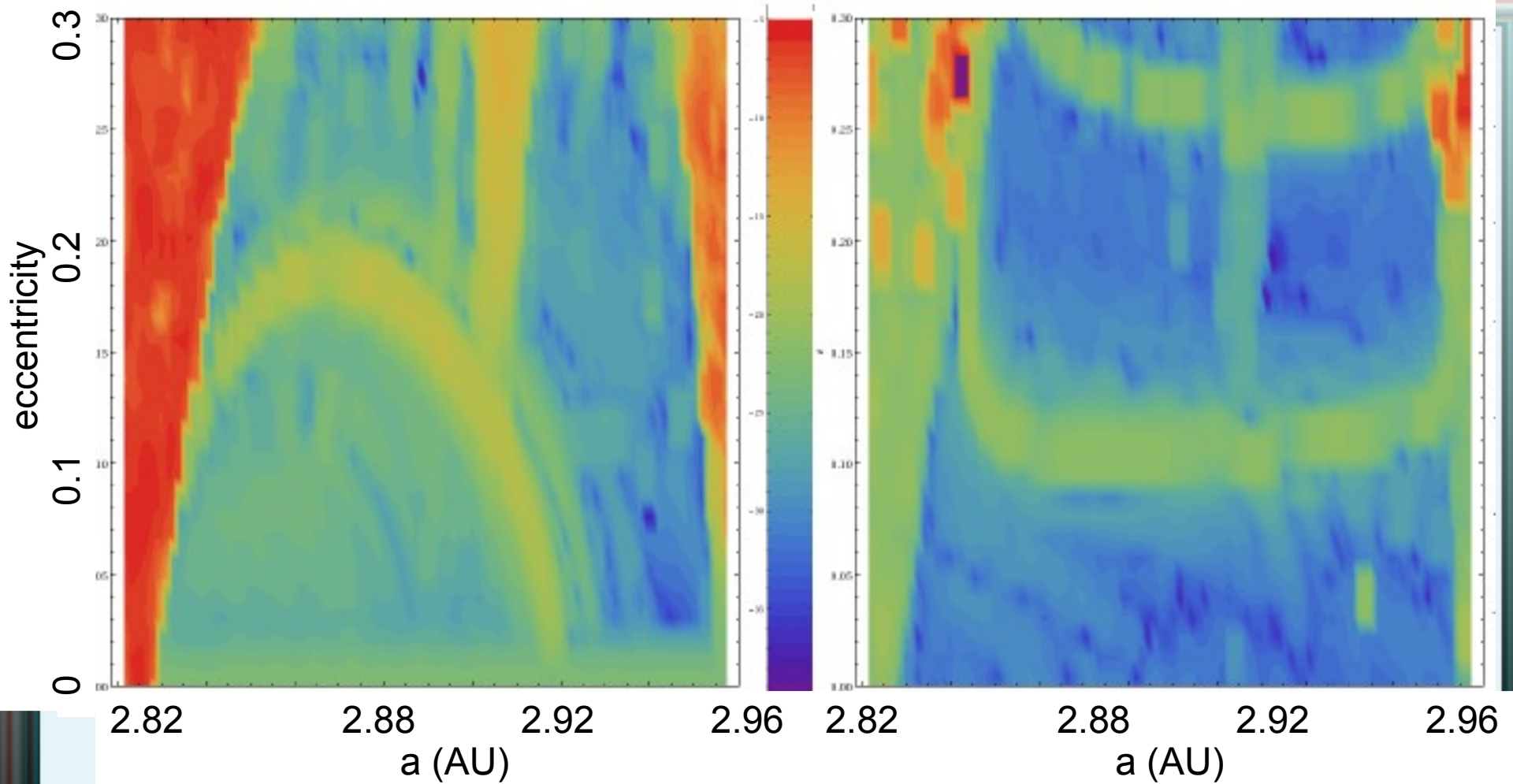
→ slide the cube (sphere..) through the data



→ and get the 'local' value of D as the slope of the msd curve

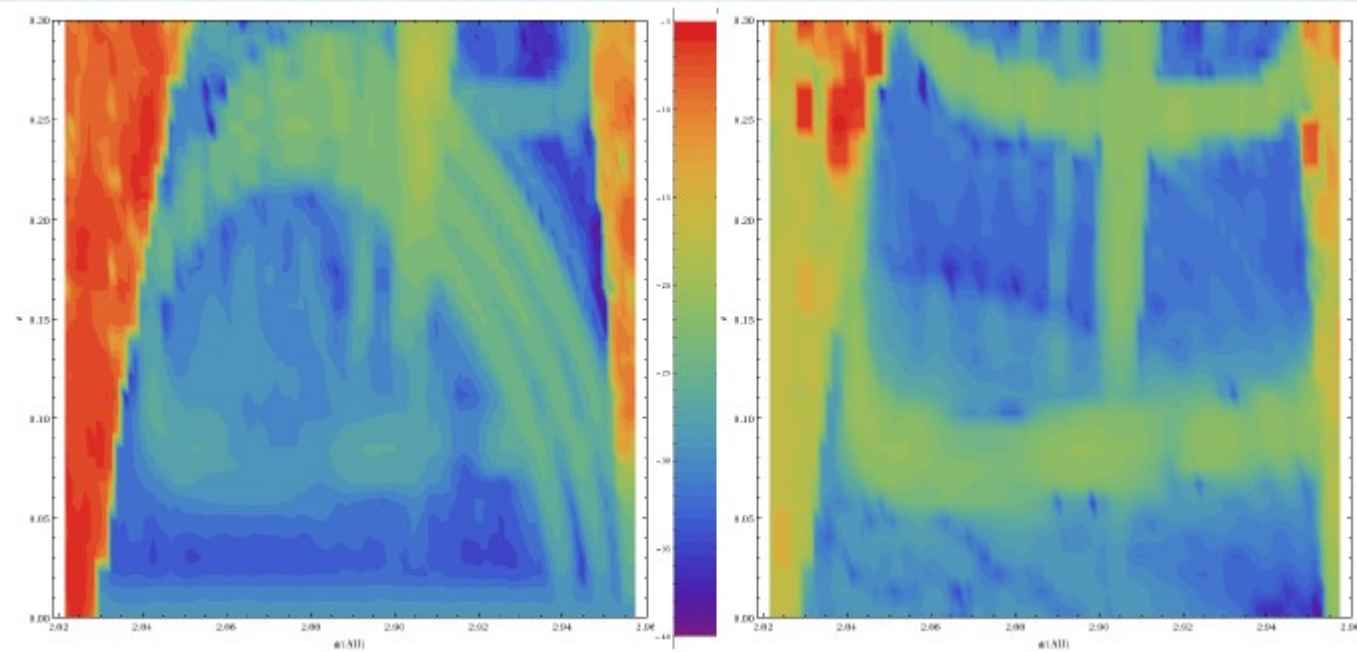
→ create a **chart** of the D values



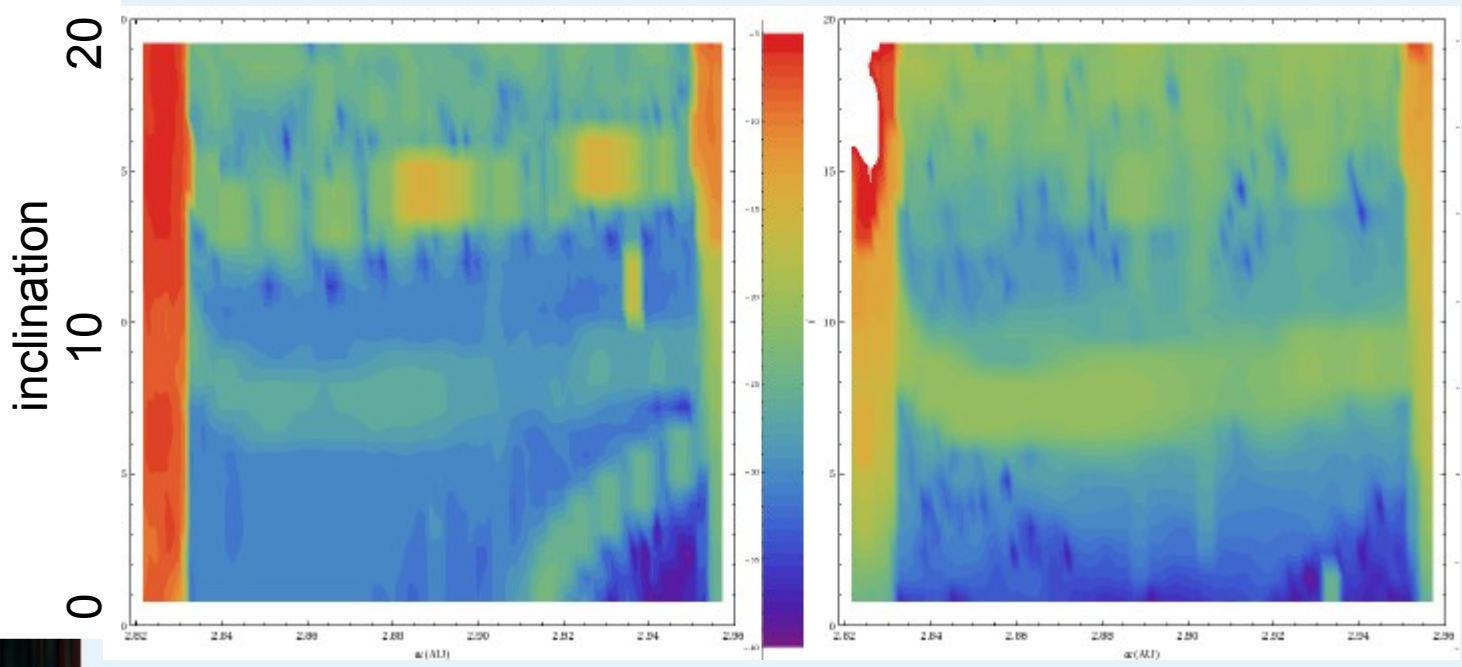


Diffusion coefficients D_e (left) and D_i (right) – 2-D projection for $0 < i < 2$ deg

- NOTE characteristic bands coinciding with resonances (MMR and sec.)
- The values increase enormously inside the 5/2 and 7/3 MMRs → will be treated as 'sinks' at the borders of the diffusion area

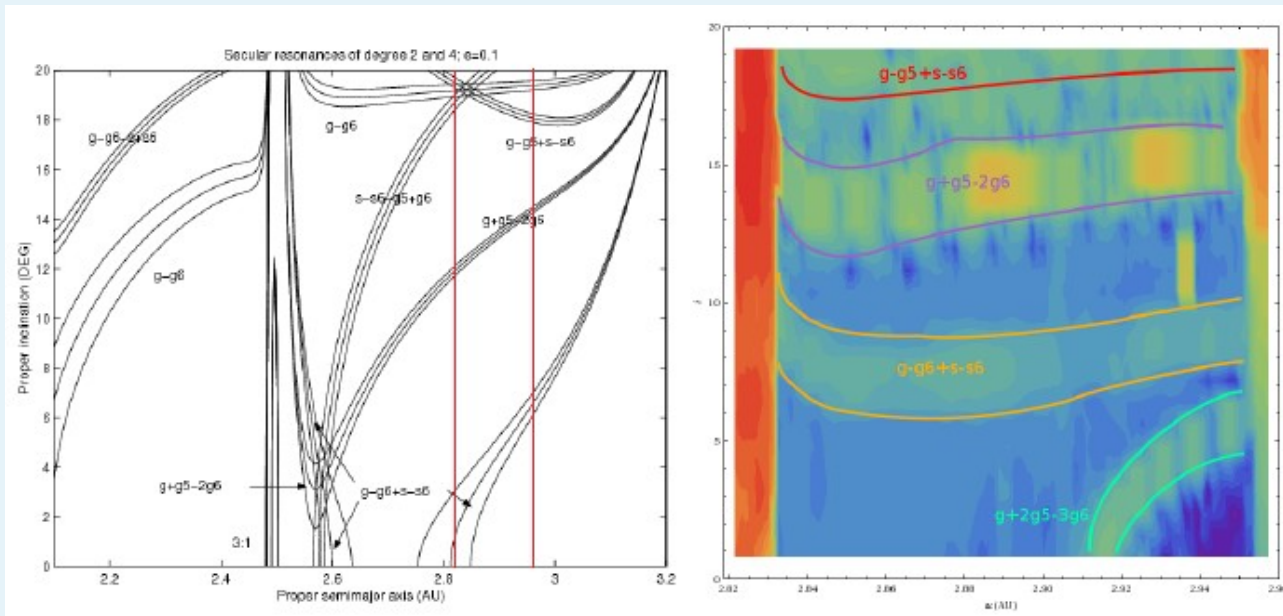


- Same projection as before (a, e) but for $i \sim 5$ deg

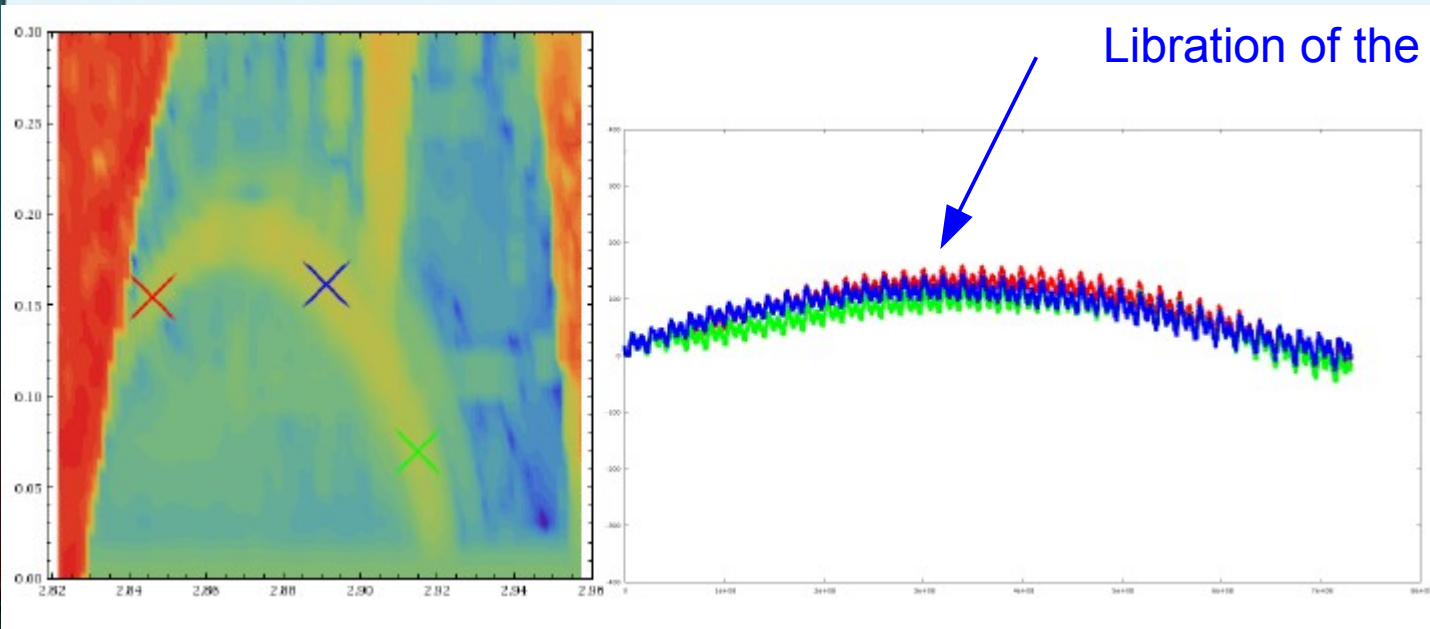


- Projection on the (a, i) plane, for $e=0.1$

Identifying secular resonances



Comparing with the Milani & Knezevic secular theory (*a-i* charts)



Libration of the critical argument

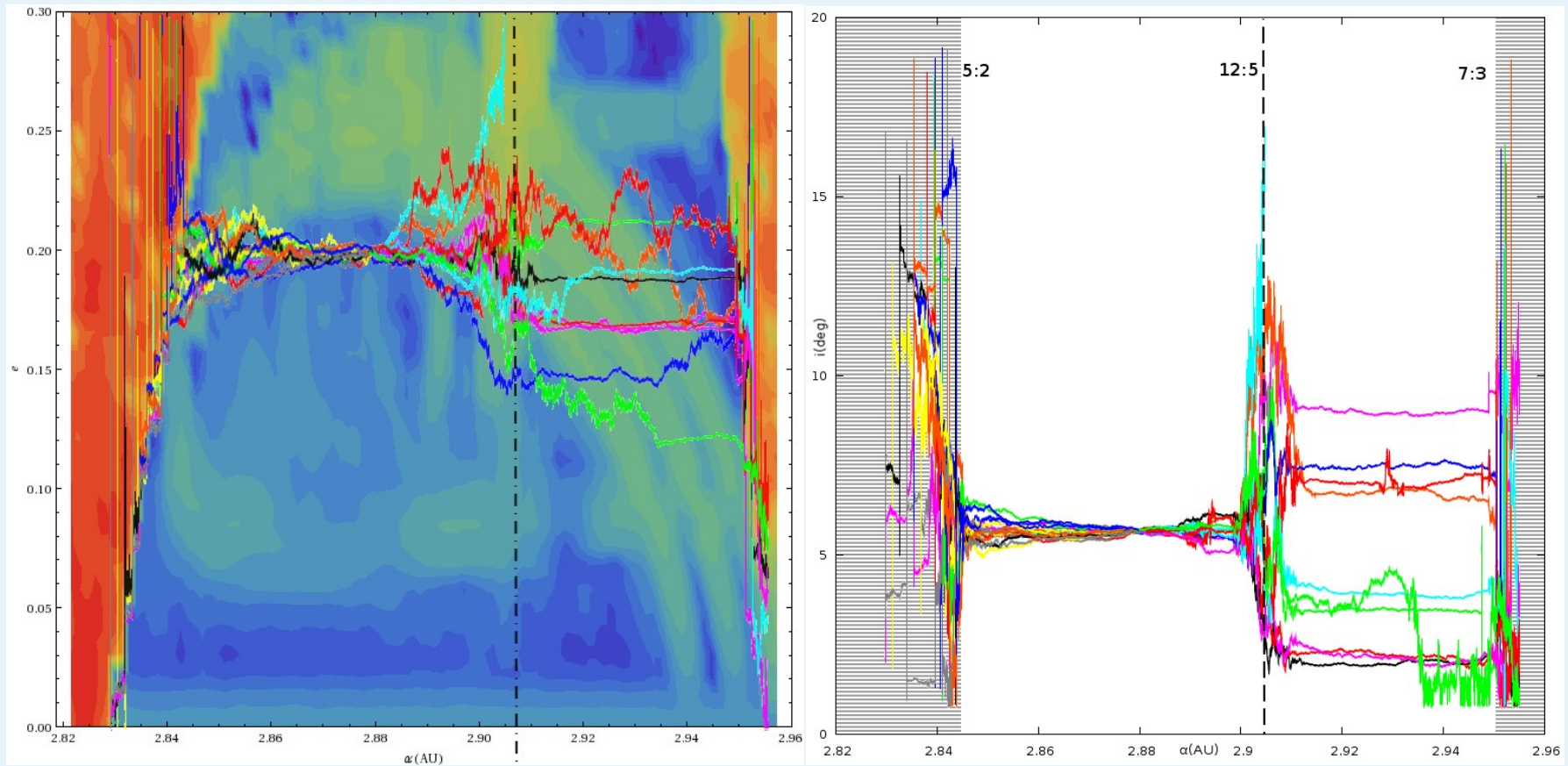
$$\varphi = \varpi + 2g_5 - 3g_6$$

(*a-e* charts)

Use D_s in a Random-Walk model

- Assume an asteroid undergoes random walk
 - 1st approximation = *normal diffusion* with the standard deviation of 'jumps' in e_p and i_p related to the local value of the diffusion coefficients
 - this can be modified (more complex random-walks) if needed
- Combine diffusion in (e_p, i_p) with drift in a (Yarkovsky) and evolution of the spin axis → at different values of a we use properly weighted values for D_s
 - at each time-step perform a jump in (e_p, i_p) according to a (local) Gaussian distribution, **plus** a displacement in a .
 - dt can be as large as a few 100 yrs, but should be small enough (according to D values) also, so that da/dt can be considered slow
- We give an initial distribution of “asteroids” and follow the evolution for 500 My (a few tens of seconds ...)

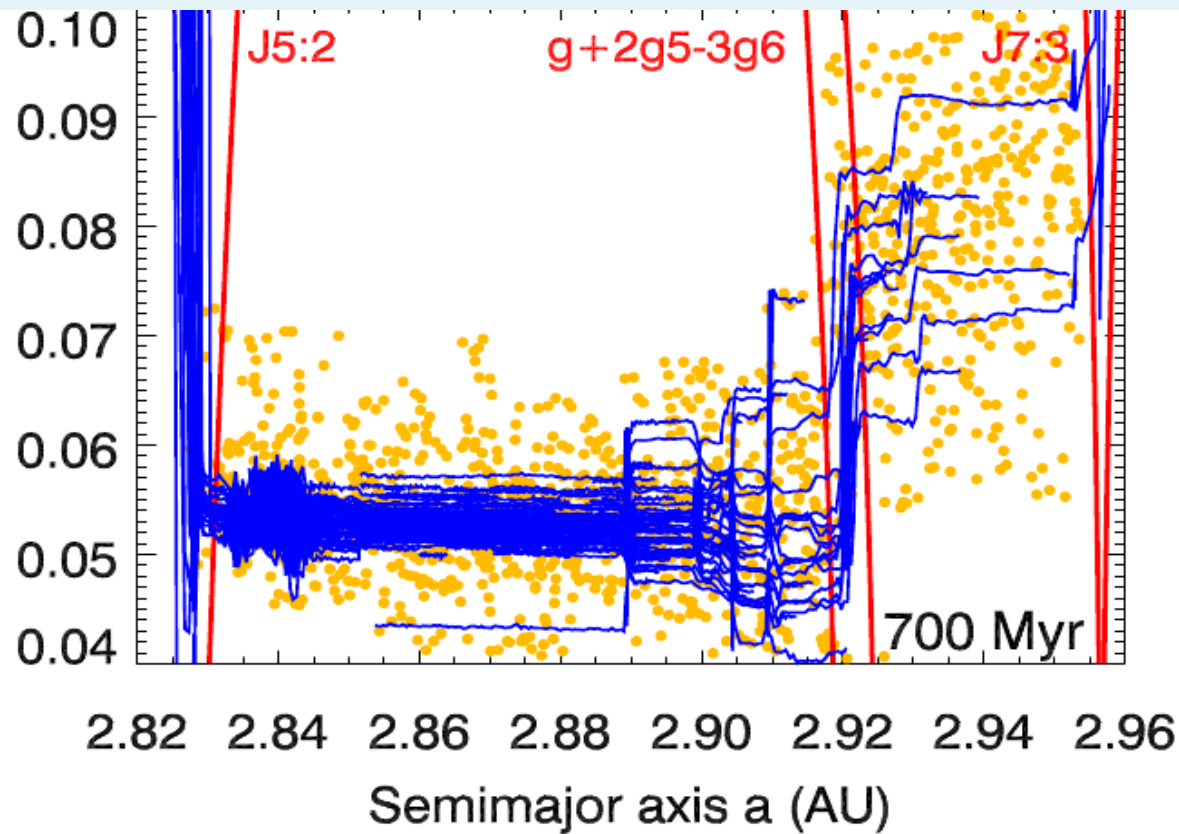
Example 1: a group of “asteroids” crossing the 12:5 MMR



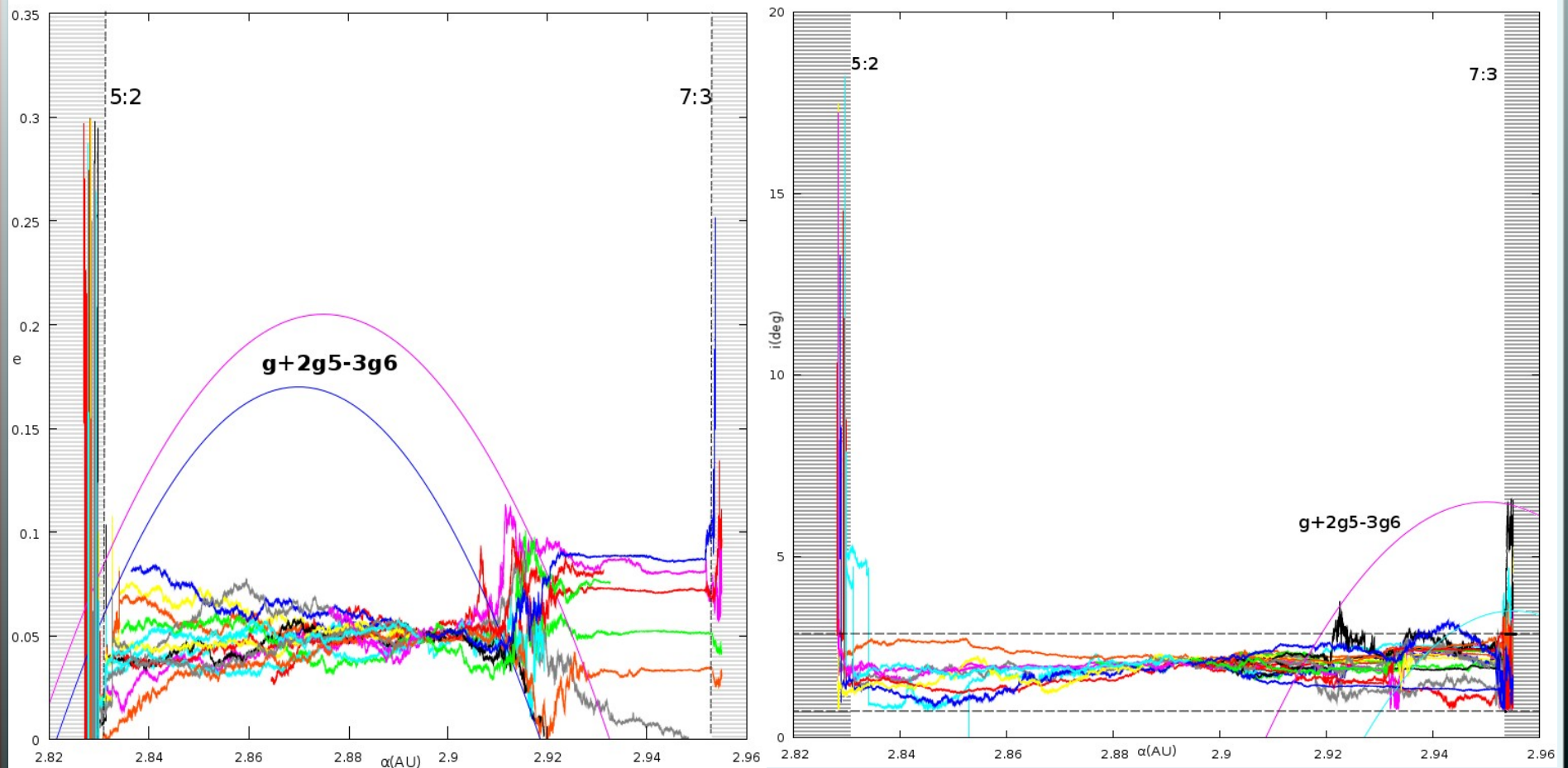
- Asteroids suffer 'jumps' in both e and i when they cross the 12/5 MMR
- Everything reaching the 5/2 and 7/3 MMRs goes 'out of the box' shortly (escape)
- Orbits with $da/dt < 0$ have only slight variations in (e, i) → no important resonances...

Example 2: application to the Koronis family (intricate shape...)

- Bottke et al. (2002) explained the shape of the Koronis family as the result of crossing the $g+2g_5-3g_6$ secular resonance due to Yarkovsky-induced drift in a



Our result (700 My simulation)



- We **reproduce** the 'jump' in e with $e_{\max} \sim 0.1$
- We **don't introduce** artificial jumps in inclination (this SR does not excite inclinations) \rightarrow same Δi on both sides...
- We **need to reduce** our "noise" level (many steps with small D)...

In sum...

- WE PLAN

to use GAIA data for asteroids (a , e , i , spin), in connection with information from other missions (albedo-size), to calculate -through an optimization process-

- (a) the *functional form of the Yarkovsky law*
- (b) the *age of families*,
- (c) the *velocity field ejection*

- METHOD

- Simulate the diffusion (in e and i) and Yarkovsky transport (in a) of an asteroid, through a random walk process, governed by
 - (i) the tabulated local diffusion coefficient (e , i)
 - (ii) the Yarkovsky law (a)

- EFFICIENCY

- FAST method: **FIRST** produce tabulated values of the diffusion coefficient $D(e, i)$ through **short-time** numerical integration of orbits, **THEN** simulate **long-time** asteroid evolution through a random walk (essentially a mapping).

- FUTURE IMPROVEMENTS

- OPTIMIZE the “selection rule” for each step, in order to attain a better match with numerical integrations.
- Reduce the noise
- Select carefully the time step...